

Synthesis of Domain Specific Encoders for Bit- Vector Solvers

Jeevana Priya Inala

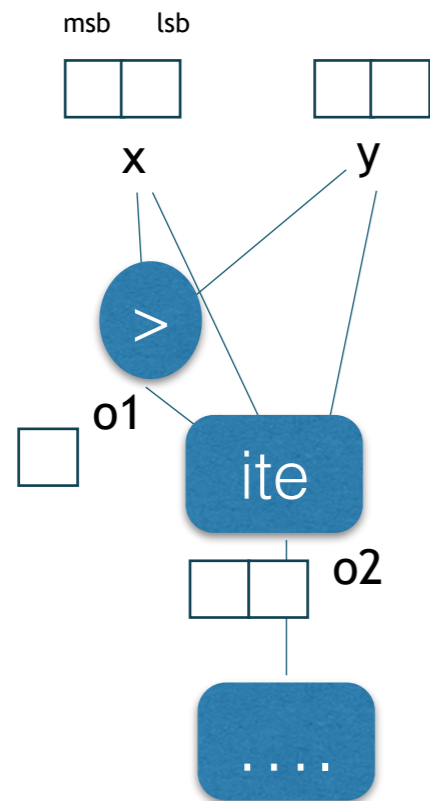
with

Rohit Singh, Armando Solar-Lezama

High-level constraint to CNF clauses

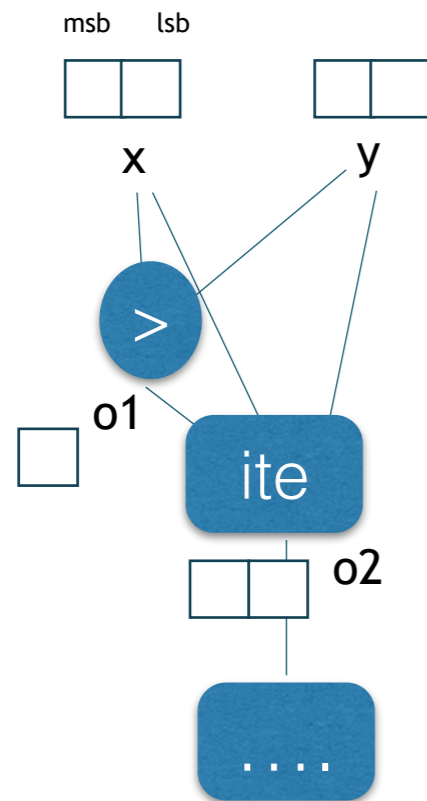
SMT solver
High-level constraint

SAT solver
CNF clauses



High-level constraint to CNF clauses

SMT solver
High-level constraint



Is this the “best” encoding?

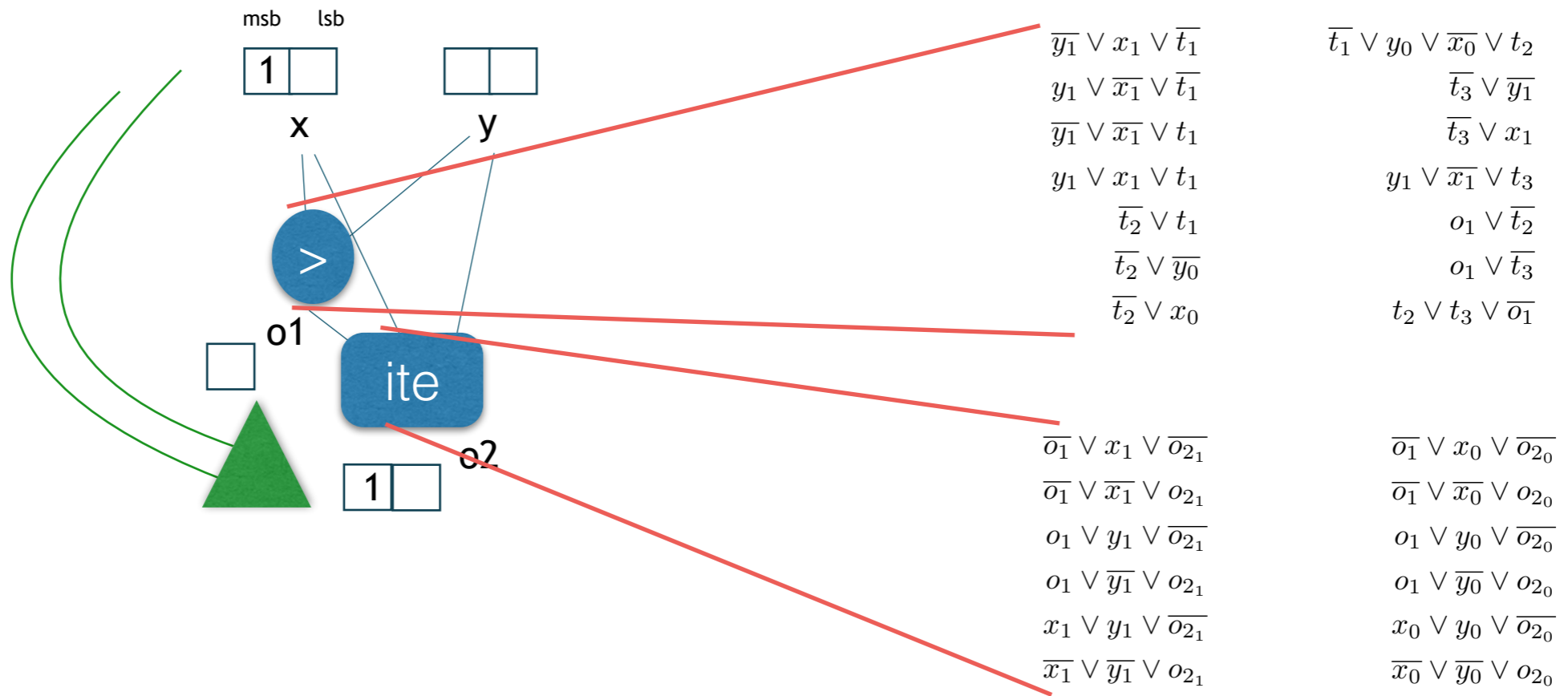
SAT solver
CNF clauses

$\bar{y}_1 \vee x_1 \vee \bar{t}_1$	$\bar{t}_1 \vee y_0 \vee \bar{x}_0 \vee t_2$
$y_1 \vee \bar{x}_1 \vee \bar{t}_1$	$\bar{t}_3 \vee \bar{y}_1$
$\bar{y}_1 \vee \bar{x}_1 \vee t_1$	$\bar{t}_3 \vee x_1$
$y_1 \vee x_1 \vee t_1$	$y_1 \vee \bar{x}_1 \vee t_3$
$\bar{t}_2 \vee t_1$	$o_1 \vee \bar{t}_2$
$\bar{t}_2 \vee \bar{y}_0$	$o_1 \vee \bar{t}_3$
$\bar{t}_2 \vee x_0$	$t_2 \vee t_3 \vee \bar{o}_1$
$\bar{o}_1 \vee x_1 \vee \bar{o}_{2_1}$	$\bar{o}_1 \vee x_0 \vee \bar{o}_{2_0}$
$\bar{o}_1 \vee \bar{x}_1 \vee o_{2_1}$	$\bar{o}_1 \vee \bar{x}_0 \vee o_{2_0}$
$o_1 \vee y_1 \vee \bar{o}_{2_1}$	$o_1 \vee y_0 \vee \bar{o}_{2_0}$
$o_1 \vee \bar{y}_1 \vee o_{2_1}$	$o_1 \vee \bar{y}_0 \vee o_{2_0}$
$x_1 \vee y_1 \vee \bar{o}_{2_1}$	$x_0 \vee y_0 \vee \bar{o}_{2_0}$
$\bar{x}_1 \vee \bar{y}_1 \vee o_{2_1}$	$\bar{x}_0 \vee \bar{y}_0 \vee o_{2_0}$
.....	

Goal: Synthesize better code for this translation

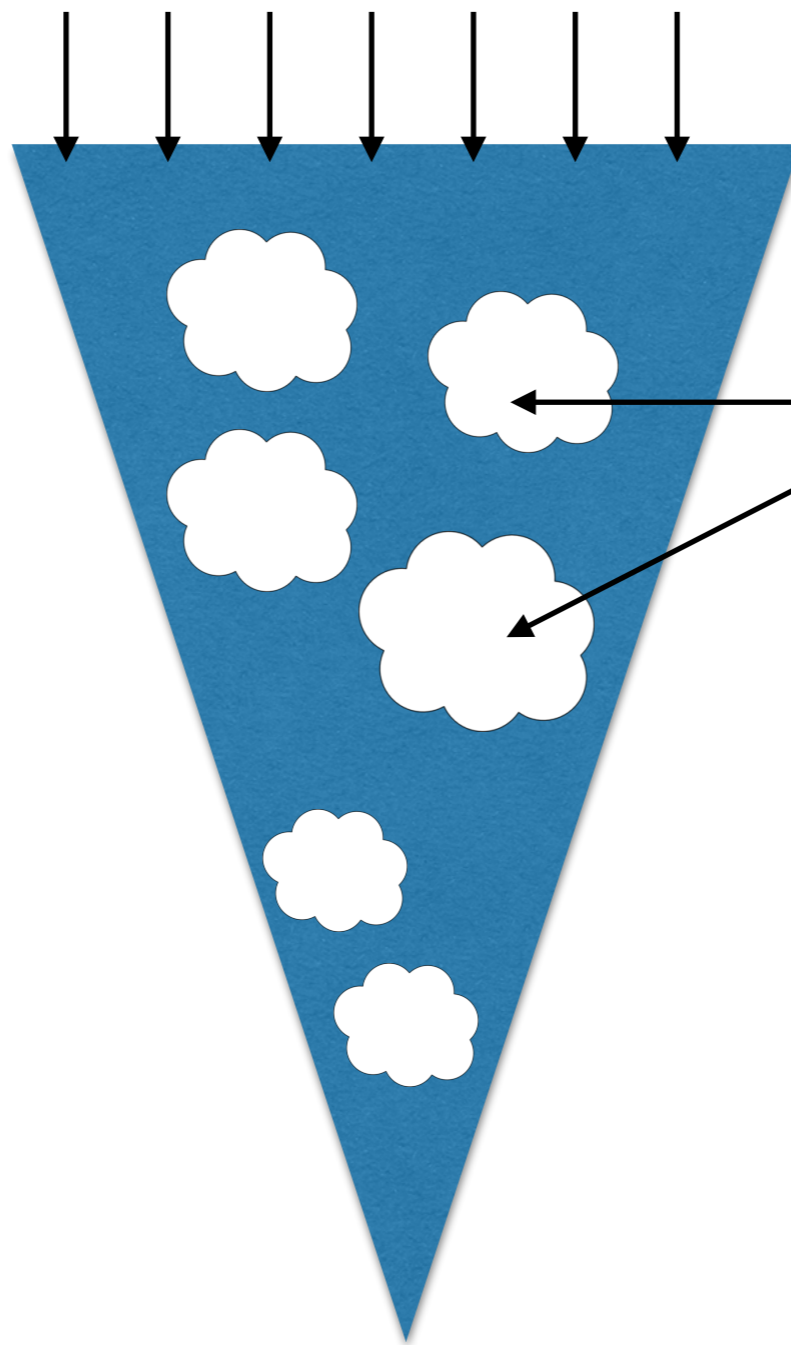
Criteria for a good encoding

- Maximal propagation
 - SAT solvers use unit propagation to infer variable assignments
 - Maximize what we learn through unit propagations
- Fewer clauses
- Fewer variables



$$x_1 = 1 \xrightarrow{\text{Unit prop}} o_{2_1} = 1$$

Composing encodings does not preserve optimality



**Focus on
optimizing
encodings for
these patterns**



What patterns to target?

How do we come up with “optimal” encoding for a pattern?

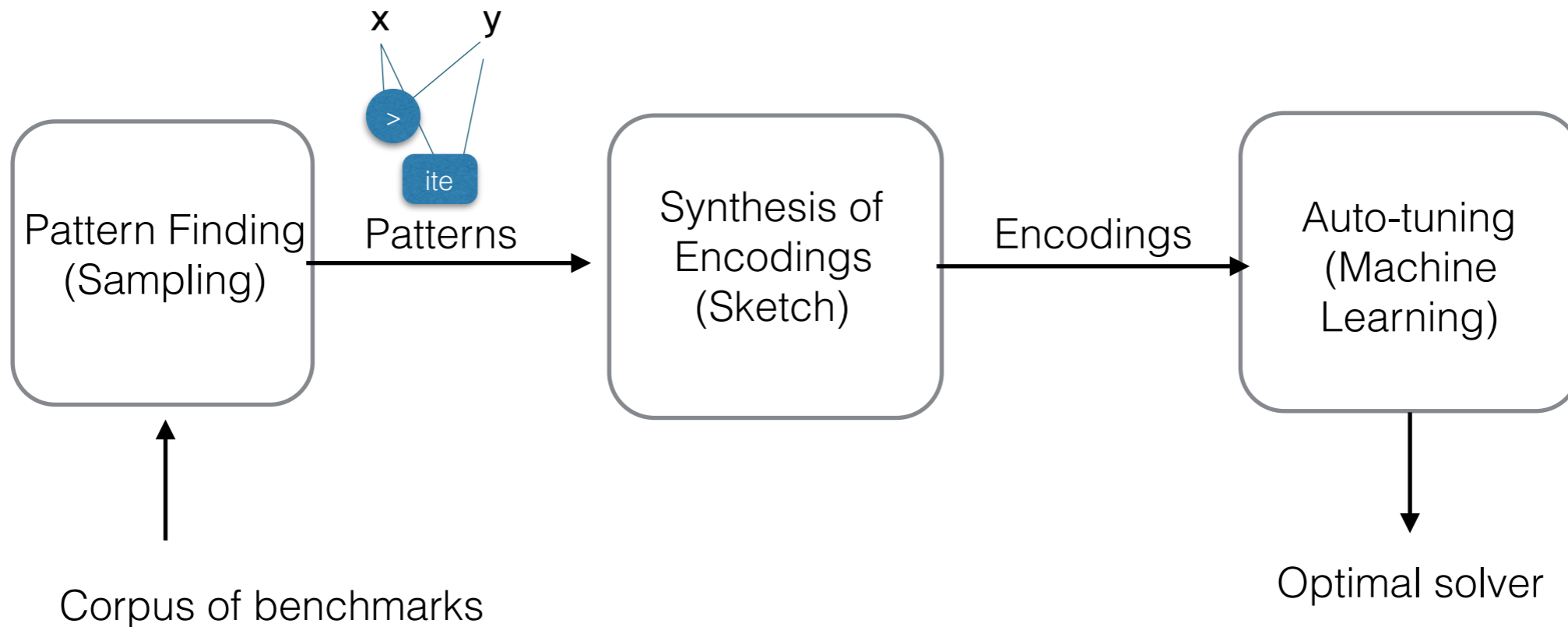
Do these encodings actually improve the performance?



What patterns to target?

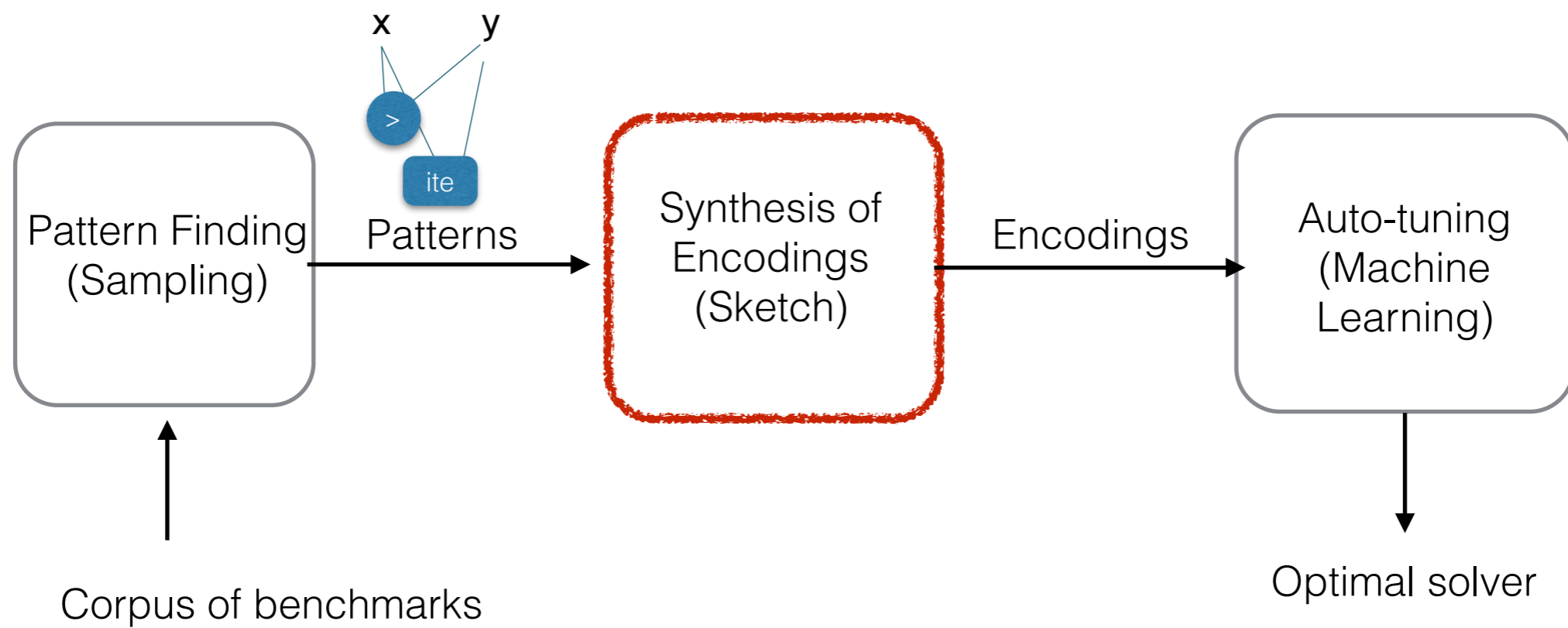
How do we come up with “optimal” encoding for a pattern?

Do these encodings actually improve the performance?



Related Work

- Automatic Generation of Propagation Complete SAT Encodings (VMCAI'16)
- Algorithm configuration for solver parameters
- Logic synthesis based SMT solvers

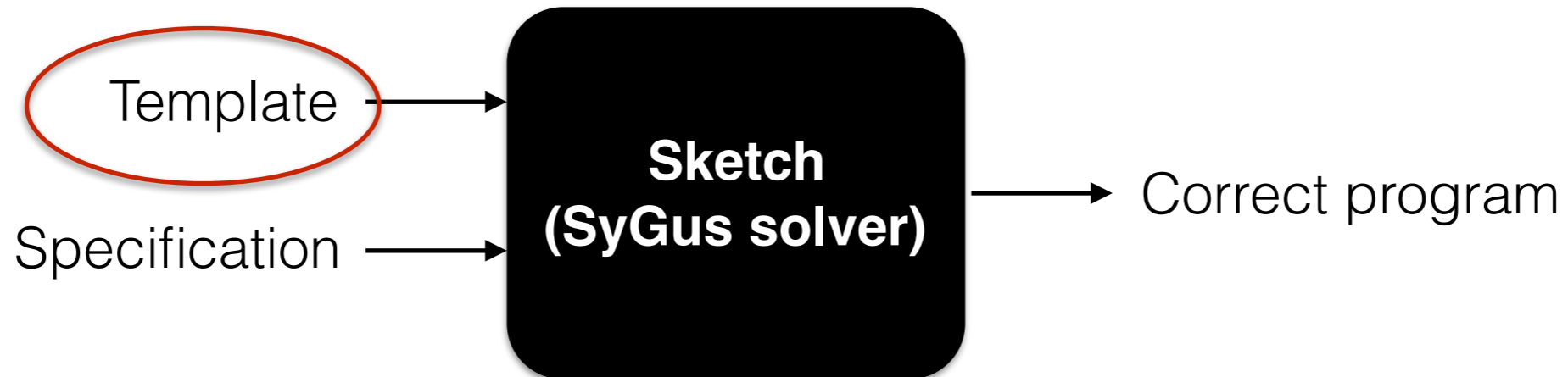


Synthesis as a SyGus problem

Boolean predicate P



CNF clauses C



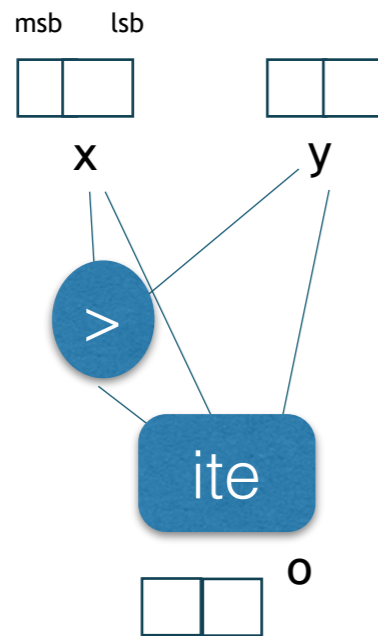
Templates

Boolean predicate P



CNF clauses C

$$o = ITE_N((GT_N x, y), x, y)$$



```
t1 = true
t2 = true
for i from N to 1 :
  t3 = newVar
  t4 = newVar
  clause({x[i], y[i], o[i]})
  clause({x[i], t1, t3})
  clause({x[i], t2, o[i], t4})
  clause({x[i], o[i], t3})
  clause({x[i], y[i], o[i]})
  clause({x[i], t2, o[i]})
  clause({x[i], t2, t4})
  clause({y[i], t2, t4})
  clause({y[i], o[i], t3})
  clause({y[i], t1, t3})
  clause({y[i], o[i], t3})
  clause({t1, t3})
  clause({t1, o[i], t3})
  clause({t2, t4})
  clause({t3, t4})
t1 = t3
t2 = t4
```

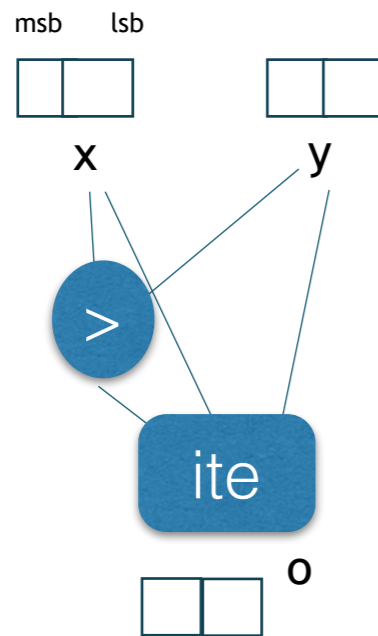
Templates

Boolean predicate P



CNF clauses C

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$t1 = true$

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for i from N to 1 :

$t3 = newVar$

$t4 = newVar$

$clause(\{x[i], y[i], \overline{o[i]}\})$

$clause(\{x[i], t1, t3\})$

$clause(\{x[i], \overline{t2}, o[i], t4\})$

$clause(\{x[i], o[i], \overline{t3}\})$

$clause(\{x[i], y[i], o[i]\})$

$clause(\{x[i], \overline{t2}, o[i]\})$

$clause(\{x[i], t2, t4\})$

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$t1 = t3$

$t2 = t4$

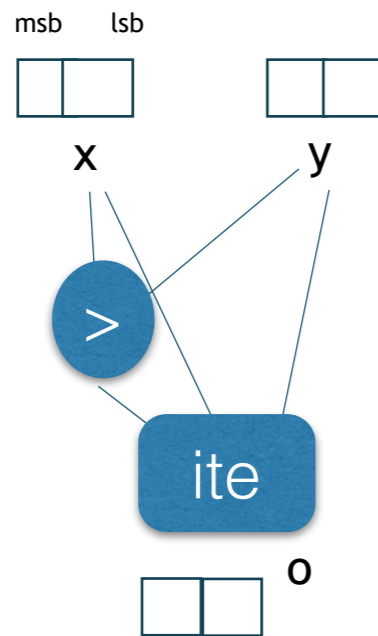
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clause({t1, t3})
clause({t1, o[i], t3})
clause({t2, t4})
clause({t3, t4})
```

$t1 = t3$

$t2 = t4$

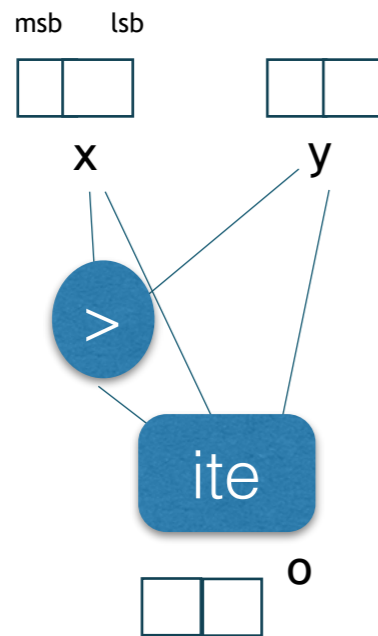
Templates

Boolean predicate P



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 $clause(\{t2, \overline{t4}\})$
 $clause(\{t3, \overline{t4}\})$

$t1 = t3$
 $t2 = t4$

Templates

$P(x, y, o)$



$t1 = ??$

$t2 = ??$

for i *from* $??$ *to* $??$:

$t3 = newVar$

$t4 = newVar$

$genClauses(x[i], y[i], o[i], t1, t2, t3, t4)$

$t1 = t3$

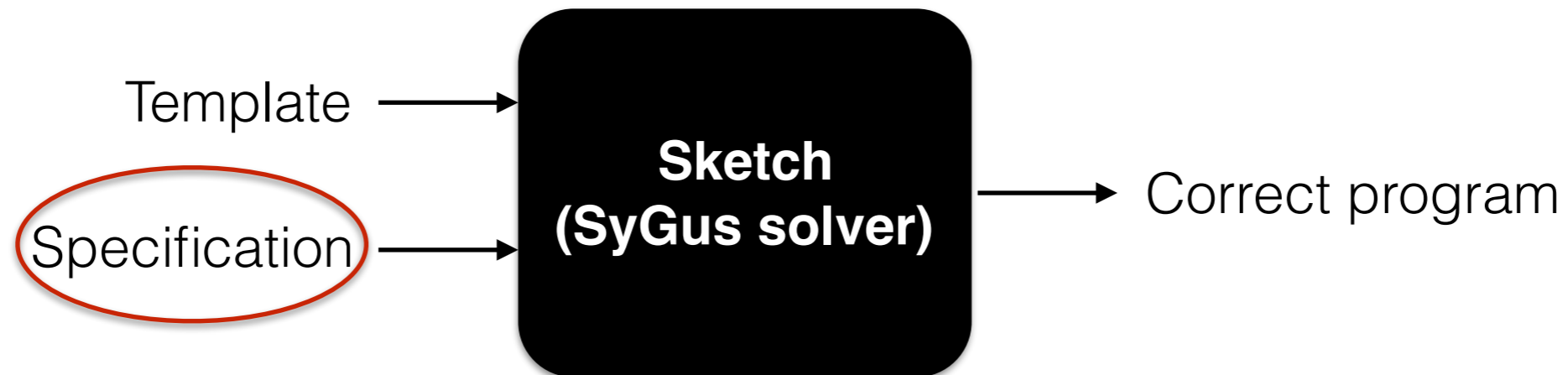
$t2 = t4$

Synthesis as a SyGus problem

Boolean predicate P



CNF clauses C



Specification

Boolean predicate P



CNF clauses C

Correctness:

$$\forall \sigma. P(\sigma) = C(\sigma)$$

σ = variables assignment

$$d = \text{ite}(a, b, c) \wedge e = d$$

$$a = T, b = T, c = F, d = T, e = T$$

$$a \vee c \vee \bar{d}$$

$$T \vee F \vee F$$

$$a \vee \bar{c} \vee d$$

$$T \vee T \vee T$$

$$\bar{a} \vee b \vee \bar{d}$$

$$F \vee T \vee F$$

$$\bar{a} \vee \bar{b} \vee d$$

$$F \vee F \vee T$$

$$P(\sigma) = C(\sigma) = T$$

$$b \vee c \vee \bar{d}$$

$$T \vee F \vee F$$

$$\bar{b} \vee \bar{c} \vee d$$

$$F \vee T \vee T$$

$$d \vee \bar{e}$$

$$T \vee F$$

$$\bar{d} \vee e$$

$$F \vee T$$

Specification

Boolean predicate P



CNF clauses C

Correctness:

$$\forall \sigma. P(\sigma) = C(\sigma)$$

σ = variables assignment

$$d = \text{ite}(a, b, c) \wedge e = d$$

$$a = F, b = T, c = F, d = T, e = T$$

$$a \vee c \vee \bar{d}$$

$$F \vee F \vee F$$

$$a \vee \bar{c} \vee d$$

$$F \vee T \vee T$$

$$\bar{a} \vee b \vee \bar{d}$$

$$T \vee T \vee F$$

$$\bar{a} \vee \bar{b} \vee d$$

$$T \vee F \vee T$$

$$P(\sigma) = C(\sigma) = F$$

$$b \vee c \vee \bar{d}$$

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$$\bar{b} \vee \bar{c} \vee d$$

$$F \vee T \vee T$$

$$d \vee \bar{e}$$

$$T \vee F$$

$$\bar{d} \vee e$$

$$F \vee T$$

Specification

Boolean predicate P



CNF clauses C

**Maximal
Propagation**

$$\forall \sigma. \text{satisfiable}(\sigma, P) \implies$$

$$d = \text{ite}(a, b, c) \wedge e = d$$

$$b = T, c = T$$

$$a \vee c \vee \bar{d}$$

$$a \vee \bar{c} \vee d$$

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Specification

Boolean predicate P



CNF clauses C

**Maximal
Propagation**

$$\forall \sigma. \text{satisfiable}(\sigma, P) \implies \\ \forall x_i, b_i. (\text{forces}(\sigma, P, x_i, b_i) \implies$$

$$d = \text{ite}(a, b, c) \wedge e = d$$

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Specification

Boolean predicate P



CNF clauses C

**Maximal
Propagation**

$$\forall \sigma. \text{satisfiable}(\sigma, P) \implies$$

$$\forall x_i, b_i. (\text{forces}(\sigma, P, x_i, b_i) \implies UP(C, \sigma) \sqsubseteq \text{extend}(\sigma, x_i, b_i))$$

$$d = \text{ite}(a, b, c) \wedge e = d$$

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Specification

Boolean predicate P



CNF clauses C

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Specification

Boolean predicate P



CNF clauses C

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Specification

Boolean predicate P



CNF clauses C

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Specification

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Difficult for synthesis tools
to reason about

Is there a better specification for maximal
propagation?

Synthesis Friendly Spec

Boolean predicate P



CNF clauses C

$$1. \forall \sigma. \text{satisfiable}(\sigma, P) \implies C(\sigma) \neq \text{false}$$

$$d = \text{ite}(a, b, c) \wedge e = d$$

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is satisfiable

No false clauses

Synthesis Friendly Spec

Boolean predicate P



CNF clauses C

1. $\forall \sigma. \text{satisfiable}(\sigma, P) \implies C(\sigma) \neq \text{false}$
2. $\forall \sigma. \text{maypropagate}(\sigma, P) \implies C(\sigma) \text{ has a unit clause}$

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Can propagate e to T

Has a unit clause

Synthesis Friendly Spec

Boolean predicate P



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$$F \vee F \vee T$$

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$$F \vee e$$

Can still propagate e to T

Has a unit clause

Synthesis Friendly Spec

Boolean predicate P



CNF clauses C

1. $\forall \sigma. \text{satisfiable}(\sigma, P) \implies C(\sigma) \neq \text{false}$
2. $\forall \sigma. \text{maypropagate}(\sigma, P) \implies C(\sigma)$ has a unit clause
3. $\forall \sigma. \text{unsatisfiable}(\sigma, P) \implies C(\sigma) = \text{false}$ (or) $C(\sigma)$ has a unit clause

$$d = \text{ite}(a, b, c) \wedge e = d$$

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$$T \vee T \vee \bar{d}$$

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Unsatisfiable

Has unit clauses

Synthesis Friendly Spec

Boolean predicate P



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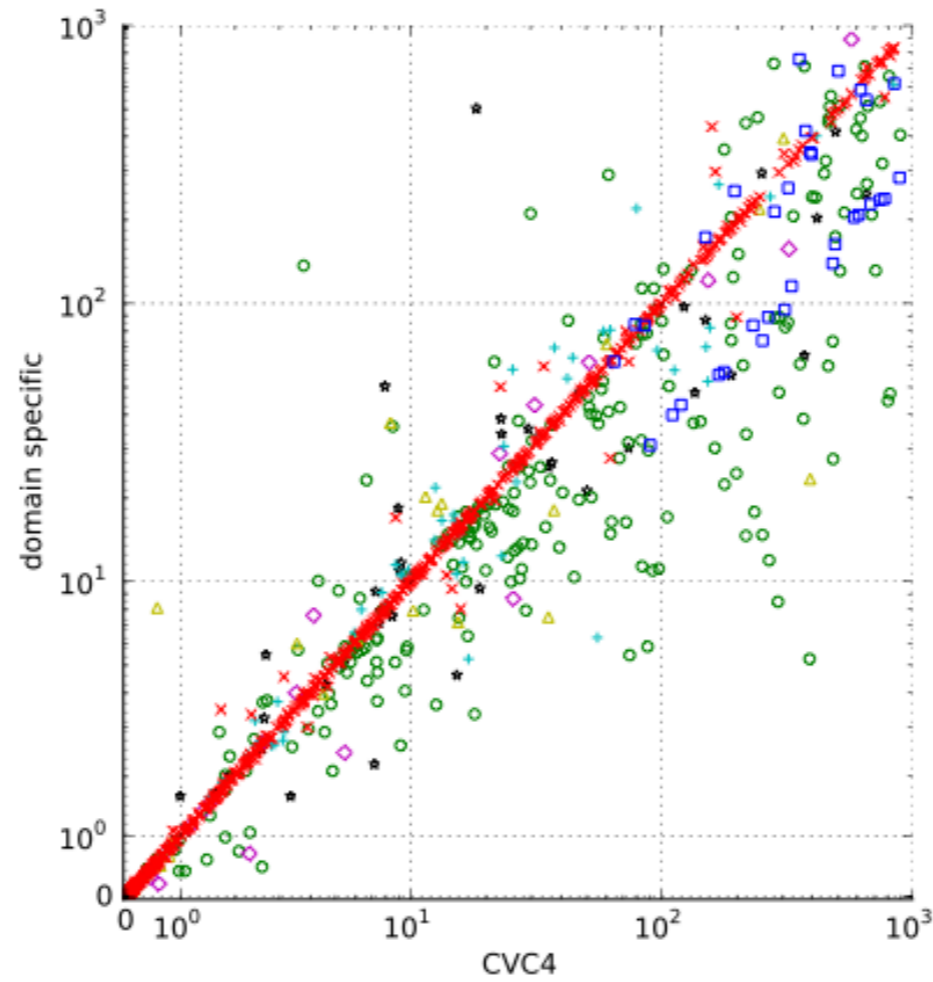
Also unsatisfiable

Has a false clause

Experimental setup

- Integrated into CVC4
- 7 domains from bit-vector category in SMT Comp'15
- Sampled ~2000 patterns (size ≤ 5)
- ~2000 SyGus problems to solve
- 8 hours of auto-tuning per domain
- On total, took 10-20 hours per domain with parallelism of 30

Does this buy you anything?



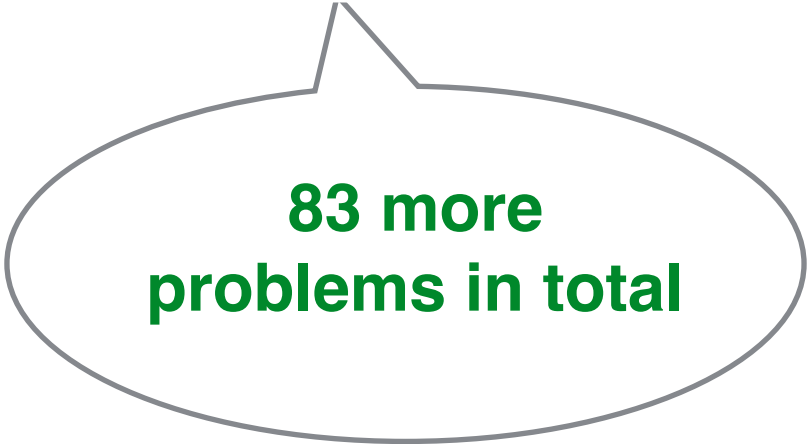
* Excluding the benchmarks used for training

Solve more problems

Benchmark Family	Solved by CVC4 →	Our Solver
<i>Log-slicing (79)</i>	33 →	62
<i>ASP (365)</i>	240 →	288
<i>Mcm (61)</i>	40 →	43
<i>Brummayerbiere2 (33)</i>	28 →	29
<i>Float (62)</i>	59 →	60
<i>Brummayerbiere3 (40)</i>	23 →	24
<i>Bruttomesso (676)</i>	623 →	623
TOTAL	1046 →	1129

Solve more problems

Benchmark Family	Solved by CVC4 →	Our Solver
<i>Log-slicing (79)</i>	33 →	62
<i>ASP (365)</i>	240 →	288
<i>Mcm (61)</i>	40 →	43
<i>Brummayerbiere2 (33)</i>	28 →	29
<i>Float (62)</i>	59 →	60
<i>Brummayerbiere3 (40)</i>	23 →	24
<i>Bruttomesso (676)</i>	623 →	623
TOTAL	1046 →	1129



**83 more
problems in total**

Solve more problems

Benchmark Family	Solved by CVC4 →	Our Solver	Boolector
<i>Log-slicing (79)</i>	33 → 62		53
<i>ASP (365)</i>	240 → 288		308
<i>Mcm (61)</i>	40 → 43		39
<i>Brummayerbiere2 (33)</i>	28 → 29		33
<i>Float (62)</i>	59 → 60		58
<i>Brummayerbiere3 (40)</i>	23 → 24		32
<i>Bruttomesso (776)</i>	623 → 623		774
TOTAL	1046 → 1129		1297

Cross domain performance

Solver Domain	→ ↓	log-slicing	asp	mcm	brumma2	float	brumma3	brutto
<i>log-slicing</i>		62	58	36	59	32	35	35
<i>asp</i>		227	288	255	227	236	253	240
<i>mcm</i>		39	38	43	40	39	39	41
<i>brumma2</i>		29	28	28	29	29	29	29
<i>float</i>		57	57	59	57	60	60	59
<i>brumma3</i>		22	22	25	22	23	24	23
<i>brutto</i>		607	606	623	609	623	623	623



Conclusion

- A framework to generate the code for translating high-level constraints to CNF
- Combined synthesis with pattern finding and auto-tuning to generate domain specific solvers
- Significant performance improvement compared to CVC4

THANK YOU

Without auto-tuning

