

Synthesis of Recursive ADT Transformations from Reusable Templates

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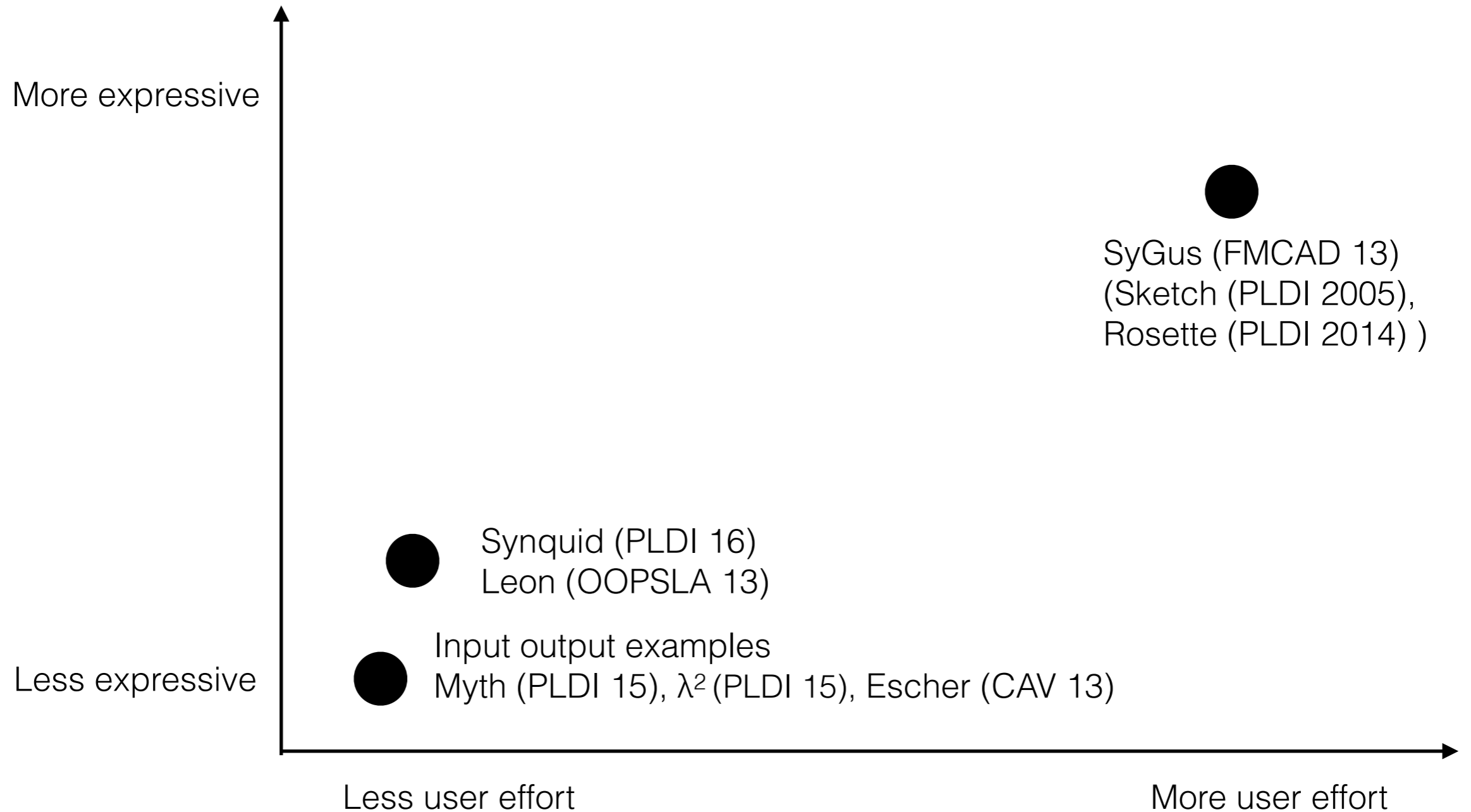
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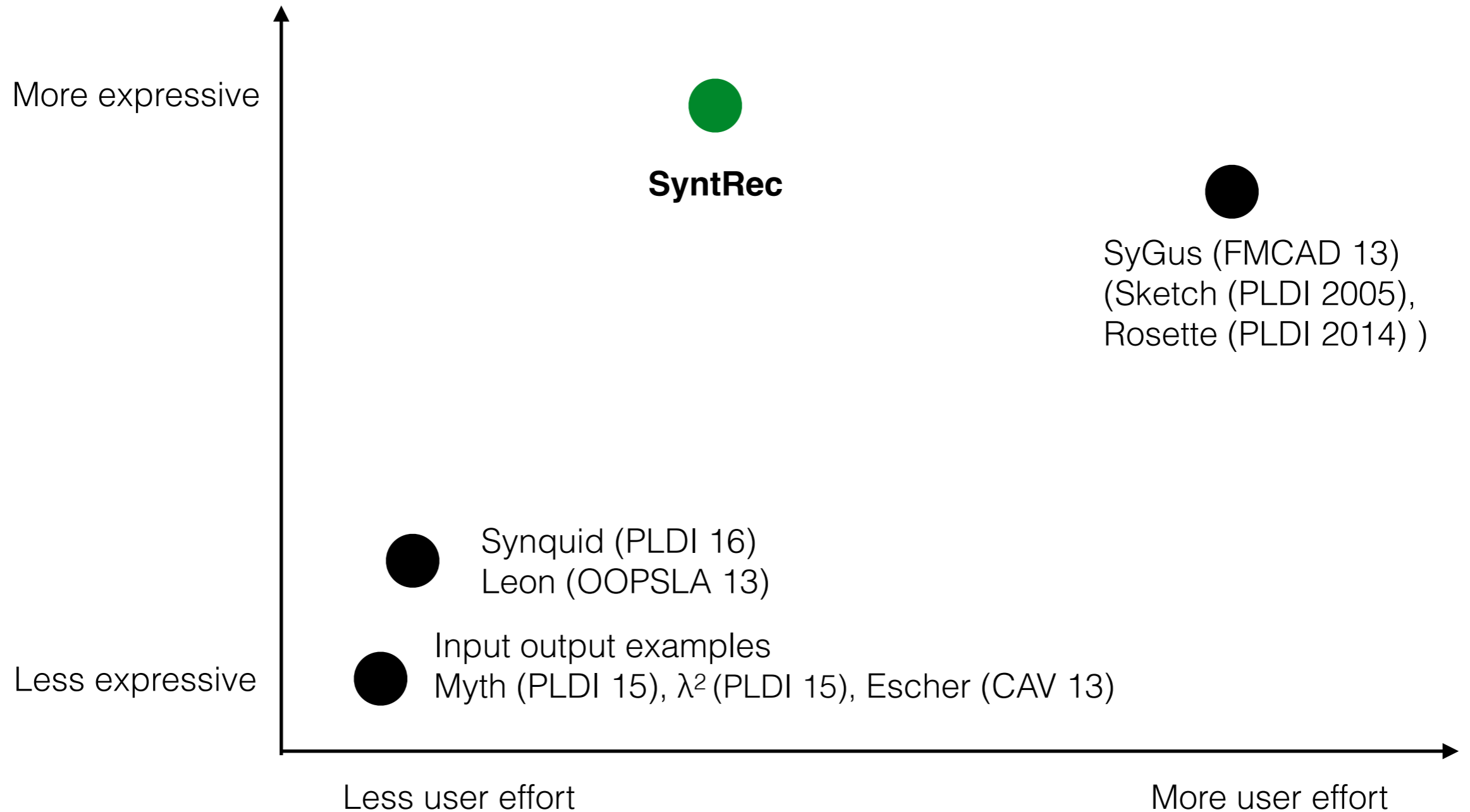


Synthesis Approaches

Synthesis Approaches



Synthesis Approaches



Recursive ADT Transformations

```
adt srcAST {  
  NumS { int v; }  
  TrueS {}  
  FalseS {}  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

```
adt dstAST {  
  NumD { int v; }  
  BoolD { bit v; }  
  BinaryD { opcode op; dstAST a; dstAST b; }  
}
```

Recursive ADT Transformations

```
adt srcAST {  
  NumS { int v; }  
  TrueS { }  
  FalseS { }  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

```
adt dstAST {  
  NumD { int v; }  
  BoolD { bit v; }  
  BinaryD { opcode op; dstAST a; dstAST b; }  
}
```

Synthesize

```
dstAST desugar(srcAST s) { .... }
```

Recursive ADT Transformations

```
adt srcAST {  
  NumS { int v; }  
  TrueS {}  
  FalseS {}  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

```
adt dstAST {  
  NumD { int v; }  
  BoolD { bit v; }  
  BinaryD { opcode op; dstAST a; dstAST b; }  
}
```

$a < b < c$

Synthesize

```
dstAST desugar(srcAST s) { .... }
```

Specification

```
interpretS(s) == interpretD(desugar(s))
```

Template in Sketch

`dstAST desugar (srcAST src)`

Template in Sketch

dstAST desugar (srcAST src)

switch (src)

case NumS:

case TrueS:

case FalseS:

case BinaryS:

case BetweenS:

Template in Sketch

dstAST desugar (srcAST src)

switch (src)

case NumS:

case TrueS:

case FalseS:

case BinaryS:

dstAST a = desugar(src.a)

dstAST b = desugar(src.b)

case BetweenS:

dstAST a = desugar(src.a)

dstAST b = desugar(src.b)

dstAST c = desugar(src.c)

Template in Sketch

```
dstAST desugar (srcAST src)
```

```
  switch (src)
```

```
    case NumS:
```

```
    case TrueS:
```

```
    case FalseS:
```

```
    case BinaryS:
```

```
      dstAST a = desugar(src.a)
```

```
      dstAST b = desugar(src.b)
```

```
    case BetweenS:
```

```
      dstAST a = desugar(src.a)
```

```
      dstAST b = desugar(src.b)
```

```
      dstAST c = desugar(src.c)
```

```
generator dstAST rcons(fun e)
```

```
  if (??)
```

```
    return e()
```

```
  if (??)
```

```
    int val = choose(e(), ??)
```

```
    return new NumD(v = val)
```

```
  if (??)
```

```
    bit val = choose(e(), ??)
```

```
    return new BoolD(v = val)
```

```
  if (??)
```

```
    dstAST a = rcons(e)
```

```
    dstAST b = rcons(e)
```

```
    opcode op = choose(e(), ??)
```

```
    return new BinaryD(op = op, a = a, b = b)
```

Template in Sketch

```
dstAST desugar (srcAST src)
  switch (src)
    case NumS:
      return rcons(()→src .v )
    case TrueS:
      return rcons(()→ 0 )
    case FalseS:
      return rcons(()→ 0 )
    case BinaryS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      return rcons(()→choose(a, b, src .op))
    case BetweenS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      dstAST c = desugar(src.c)
      return rcons(()→choose(a, b, c ))
```

```
generator dstAST rcons(fun e)
  if (??)
    return e()
  if (??)
    int val = choose(e(), ??)
    return new NumD(v = val)
  if (??)
    bit val = choose(e(), ??)
    return new BoolD(v = val)
  if (??)
    dstAST a = rcons(e)
    dstAST b = rcons(e)
    opcode op = choose(e(), ??)
    return new BinaryD(op = op, a = a, b = b)
```

Template in Sketch

```
dstAST desugar (srcAST src)
  switch (src)
    case NumS:
      return rcons(()→src .v )
    case TrueS:
      return rcons(()→ 0 )
    case FalseS:
      return rcons(()→ 0 )
    case BinaryS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      return rcons(()→choose(a, b, src .op))
    case BetweenS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      dstAST c = desugar(src.c)
      return rcons(()→choose(a, b, c ))
```

```
generator dstAST rcons(fun e)
  if (??)
    return e()
  if (??)
    int val = choose(e(), ??)
    return new NumD(v = val)
  if (??)
    bit val = choose(e(), ??)
    return new BoolD(v = val)
  if (??)
    dstAST a = rcons(e)
    dstAST b = rcons(e)
    opcode op = choose(e(), ??)
    return new BinaryD(op = op, a = a, b = b)
```

No. of possible functions from template ~ 2^{110}

Template in Sketch

```
dstAST desugar (srcAST src)
  switch (src)
    case NumS:
      return rcons(()→src .v )
    case TrueS:
      return rcons(()→ 0 )
    case FalseS:
      return rcons(()→ 0 )
    case BinaryS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      return rcons(()→choose
    case BetweenS:
      dstAST a = desugar(src.a)
      dstAST b = desugar(src.b)
      dstAST c = desugar(src.c)
      return rcons(()→choose(a, b, c ))
```

```
generator dstAST rcons(fun e)
  if (??)
    return e()
  if (??)
    int val = choose(e(), ??)
    return new NumD(v = val)
  if (??)
    bit val = choose(e(), ??)
    return new BoolD(v = val)
  if (??)
    dstAST a = rcons(e)
    dstAST b = rcons(e)
    pcode op = choose(e(), ??)
    return new BinaryD(op = op, a = a, b = b)
```

Verbose

Not reusable

No. of possible functions from template ~ 2^{110}

Reusable Templates

- ***Polymorphic synthesis constructs*** to support general operations on ADTs

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

```
P = dstAST
Q = srcAST
replacer = desugar
```

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
```

Polymorphic Generator

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

```
P = dstAST
Q = srcAST
replacer = desugar
```

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
```

Flexible pattern matching

```
src :: srcAST
```

```
cases?: e
```

```
case Nums: e
```

```
case TrueS: e
```

```
case FalseS: e
```

```
case BinaryS: e
```

```
case BetweenS: e
```

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

P = dstAST
Q = srcAST
replacer = desugar

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
    P[ ] a = map(src.fields?, replacer )
```

Fields list

```
case BinaryS:
  dstAST[ ] a = map(src.fields?, desugar )
```

```
src :: BinaryS{opcode op;
  srcAST a; srcAST b;}
```

src.**fields?** → { src.a, src.b }

```
src.fields? :: srcAST[ ]
```

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

P = dstAST
Q = srcAST
replacer = desugar

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
    P[ ] a = map(src.fields?, replacer )
```

Fields list

```
case NumS:
  dstAST[ ] a = map(src.fields?, desugar )
```

src :: NumS{ int v; }

src.fields? :: srcAST[]

src.**fields?** → {}

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

```
P = dstAST
Q = srcAST
replacer = desugar
```

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
    P[ ] a = map(src.fields?, replacer )
    return rcons(()→choose(a[??], field ( src )))
```

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

```
P = dstAST
Q = srcAST
replacer = desugar
```

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
    P[ ] a = map(src.fields?, replacer )
    return rcons(()→choose(a[??], field ( src )))
```

```
generator T field <T,S> (S e)
  return (e.fields?)[??];
```

Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

P = dstAST
Q = srcAST
replacer = desugar

```
generator T rcons <T> (fun e)
  if (??)
    return e();
  else
    return new cons?(rcons(e));
```

Unknown Constructor

T = dstAST

```
cons?(rcons(e)) → choose( new NumD(v = rcons(e)),
  .....,
  new BinaryD(op = rcons(e),
    a = rcons(e), b = rcons(e)))
```

Polymorphic Synthesis Constructs (PSCs)

- Polymorphic generators
- Flexible pattern matching

switch (e₁) **case?** e₂

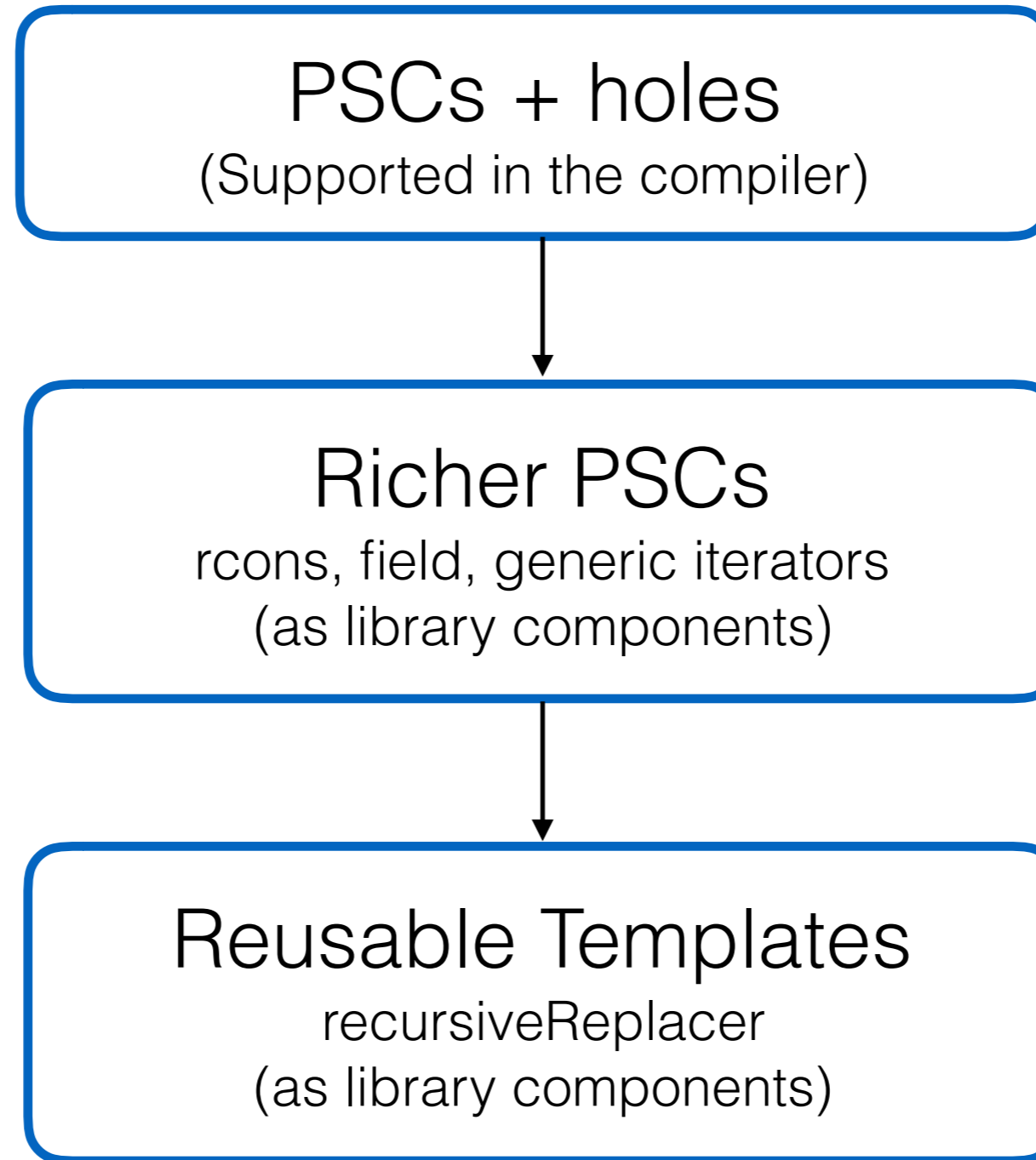
- Fields list

e.**fields?**

- Unknown constructor

cons?(e₁, e₂, ... e_k)

Combinations of PSCs



Reusable Templates

```
dstAST desugar (srcAST src)
  return recursiveReplacer ( src , desugar)
```

```
P = dstAST
Q = srcAST
replacer = desugar
```

```
generator P recursiveReplacer <P, Q> (Q src, fun replacer)
  switch(src)
  cases?:
    P[ ] a = map(src.fields?, replacer )
    return rcons(()→choose(a[??], field ( src )))
```

Concise

Reusable

Reusable Templates

Synthesized program for desugar

```
dstAST desugar (srcAST src)
  switch (src)
    case NumS: return new NumD(v = src.v)
    case TrueS: return new BoolD(v = 1)
    case FalseS: return new BoolD(v = 0)
    case BinaryS:
      dstAST[2] a = {desugar(src.a), desugar(src .b)}
      return new BinaryD(op = src.op, a = a[1], b = a [2])
    case BetweenS:
      dstAST[3] a = {desugar(src.a), desugar(src .b), desugar(src .c)}
      return new BinaryD(op = new AndOp(),
        a = new BinaryD(op = new LtOp(), a = a[0], b = a[1]),
        b = new BinaryD(op = new LtOp(), a = a[1], b = a [2]))
```

Synthesis Time: 8s

Reusable Templates

Synthesized program for desugar

```
dstAST desugar (srcAST src)
  switch (src)
    case NumS: return new NumD(v = src.v)
    case TrueS: return new BoolD(v = 1)
    case FalseS: return new BoolD(v = 0)
    case BinaryS:
      dstAST[2] a = {desugar(src.a), desugar(src .b)}
      return new BinaryD(op = src.op, a = a[1], b = a [2])
    case BetweenS:
      dstAST[3] a = {desugar(src.a), desugar(src .b), desugar(src .c)}
      return new BinaryD(op = new AndOp(),
        a = new BinaryD(op = new LtOp(), a = a[0], b = a[1]),
        b = new BinaryD(op = new LtOp(), a = a[1], b = a [2]))
```

Synthesis Time: 8s

Reusable Templates

Church encoding for Boolean operations

```
adt Bool {  
  True {}  
  False {}  
  And { Bool a; Bool b; }  
  Or { Bool a; Bool b; }  
  Not { Bool a; }  
}
```

```
adt E {  
  Var { int v; }  
  Abs { Var v; E a }  
  App { E a; E b; }  
}
```

```
E desugar (Bool src)  
  return recursiveReplacer ( src , desugar)
```

Reusable Templates

Synthesized program for Church encodings for Boolean operations

E desugar (Bool src)

switch (src)

case True: **return new** Abs(**new** Var(0), **new** Abs(**new** Var(1), **new** Var(0)))

case False: **return new** Abs(**new** Var(0), **new** Abs(**new** Var(1), **new** Var(1)))

case And:

E[2] a = { desugar(src.a), desugar(src.b) }

return new App(**new** App(a[0], a[1]), a[0])

case Or:

E[2] a = { desugar(src.a), desugar(src.b) }

return new App(**new** App(a[0], a[0]), a[1])

case Not:

E[1] a = { desugar(src.a) }

return new App(**new** App(a[0], **new** Abs(**new** Var(0), **new** Abs(**new** Var(1), **new** Var(0)))), **new** Abs(**new** Var(0), **new** Abs(**new** Var(1), **new** Var(1))))

Synthesis Time: 43s

Reusable Templates

generator P recursiveReplacer <P, Q> (Q src, **fun** replacer, **fun** condGen, **fun** fieldGen)

switch(src)

cases?:

P[] a = map(src.**fields?**, replacer)

repeat

if (condGen(field(src))

return rcons(()→**choose**(a[??], field (src), fieldGen()))

Reusable Templates

generator P recursiveReplacer <P, Q> (Q src, **fun** replacer, **fun** condGen, **fun** fieldGen)

switch(src)

cases?:

P[] a = map(src.**fields?**, replacer)

repeat

if (condGen(field(src))

return rcons(()→**choose**(a[??], field (src), fieldGen()))

dstAST desugar (srcAST src)

return recursiveReplacer (src , desugar, ()→**true**, ()→0)

Btree insert (Btree tree, **int** x)

return recursiveReplacer (tree , (t)->insert(t, x),
(v)→**choose**(v <= x, v > x, **true**),
(->x)

Reusable Templates

Synthesized program for binary tree insertion

```
BTree insert (BTree tree, int x)
  switch (src)
    case Branch:
      BTree[2] a = {insert(tree.left, x), insert(tree.right, x)}
      if (tree.val <= x)
        return new BTree(tree.val, a[0], tree.right)
      if (tree.val > x)
        return new BTree(tree.val, tree.left, a[1])
    case Leaf:
      if (tree.val <= x)
        return new BTree(x, new Leaf(tree.v), new Empty())
      if (tree.val > x)
        return new BTree(x, new Empty(), new Leaf(tree.v))
    case Empty:
      return new Leaf(x)
```

Synthesis Time: 20s

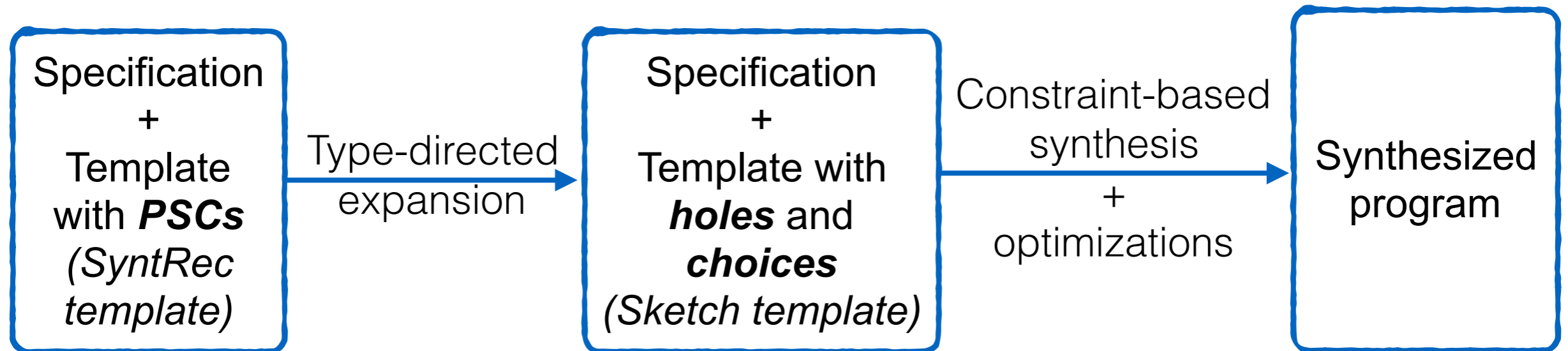
Reusable Templates

Synthesized program for binary tree insertion

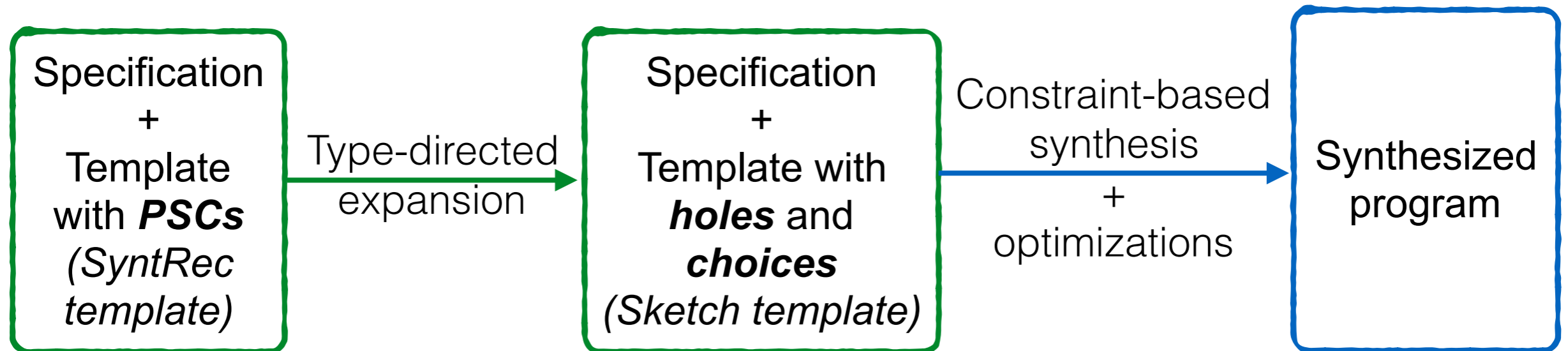
```
BTree insert (BTree tree, int x)
  switch (src)
    case Branch:
      BTree[2] a = {insert(tree.left, x), insert(tree.right, x)}
      if (tree.val <= x)
        return new BTree(tree.val, a[0], tree.right)
      if (tree.val > x)
        return new BTree(tree.val, tree.left, a[1])
    case Leaf:
      if (tree.val <= x)
        return new BTree(x, new Leaf(tree.v), new Empty())
      if (tree.val > x)
        return new BTree(x, new Empty(), new Leaf(tree.v))
    case Empty:
      return new Leaf(x)
```

Synthesis Time: 20s

Synthesis Approach

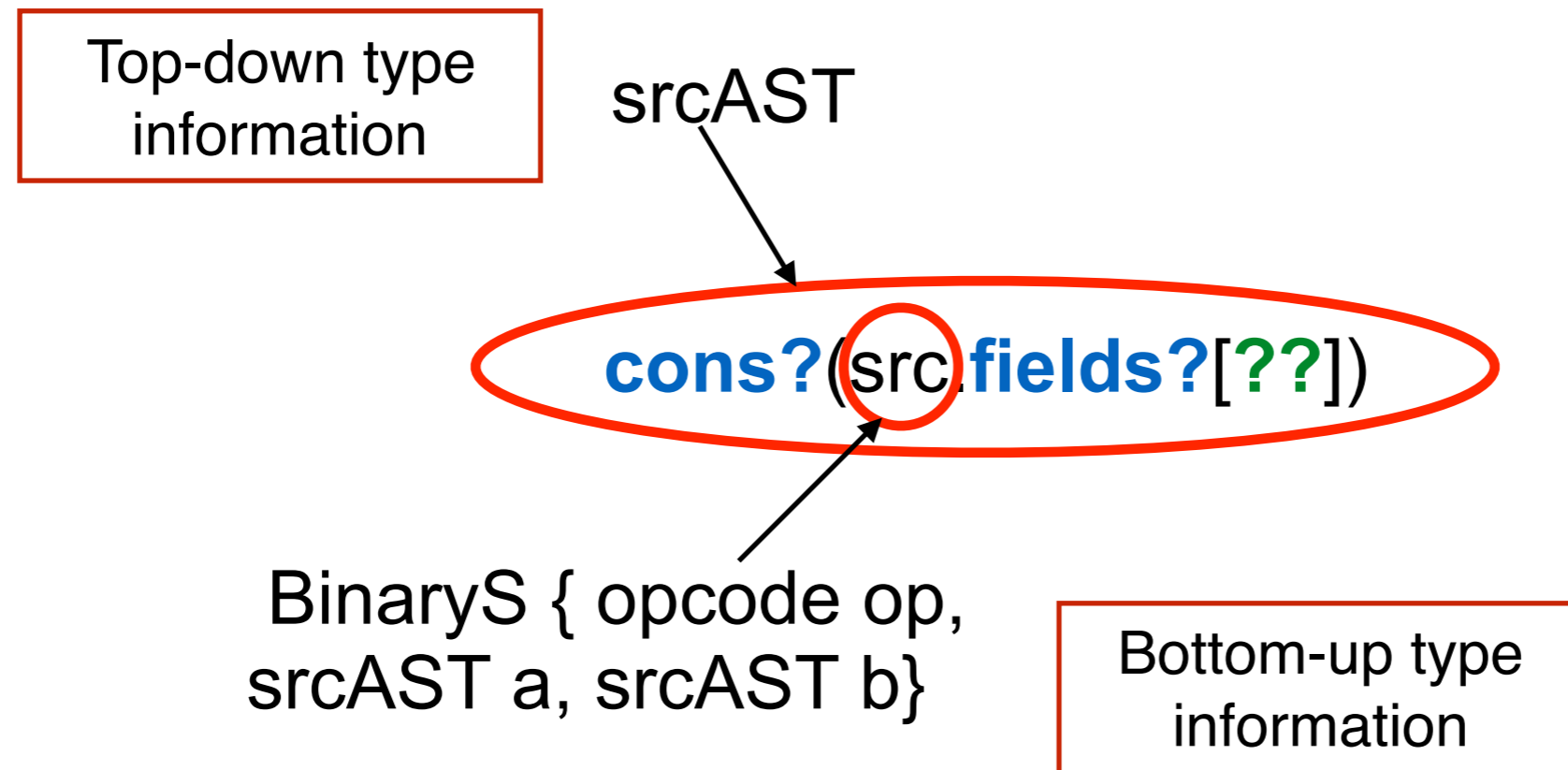


Synthesis Approach



Type-directed expansion

Requires propagating type information both top-down and bottom-up



Type-directed expansion

- Bi-directional rules of Pierce and Turner, 2000
- Also used in Myth (PLDI 2015) and Synquid (PLDI 2016)

Type Inference rule

$$\Gamma \vdash e : \theta$$

Expansion rule

$$\Gamma \vdash e \xrightarrow{\theta} e'$$

Type-directed expansion

`cons?(src.fields?[??])` $\xrightarrow{\text{srcAST}}$

```
adt srcAST {  
  NumS { int v; }  
  TrueS {}  
  FalseS {}  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

Type-directed expansion

`cons?(src.fields?[??])` $\xrightarrow{\text{srcAST}}$ `choose (new NumS(...),
new BinaryS(...),
...)`

```
adt srcAST {  
  NumS { int v; }  
  TrueS {}  
  FalseS {}  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

Type-directed expansion

`cons?(src.fields?[??])` $\xrightarrow{\text{srcAST}}$ `choose (new NumS(...),
new BinaryS(a = src.fields?[??], ...),
...)`

`src.fields?[??]` $\xrightarrow{\text{srcAST}}$

`src.fields?` $\xrightarrow{\text{srcAST}[]}$

```
adt srcAST {  
  NumS { int v; }  
  TrueS { }  
  FalseS { }  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```


Type-directed expansion

`cons?(src.fields?[??])` $\xrightarrow{\text{srcAST}}$ `choose (new NumS(...),
new BinaryS(a = src.fields?[??], ...),
...)`

`src.fields?[??]` $\xrightarrow{\text{srcAST}}$

`src.fields?` $\xrightarrow{\text{srcAST}[]}$

`src` $\xrightarrow{\text{BinaryS}}$ `src`

```
adt srcAST {  
  NumS { int v; }  
  TrueS { }  
  FalseS { }  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

Type-directed expansion

`cons?(src.fields?[??])` $\xrightarrow{\text{srcAST}}$ `choose (new NumS(...),
new BinaryS(a = src.fields?[??], ...),
...)`

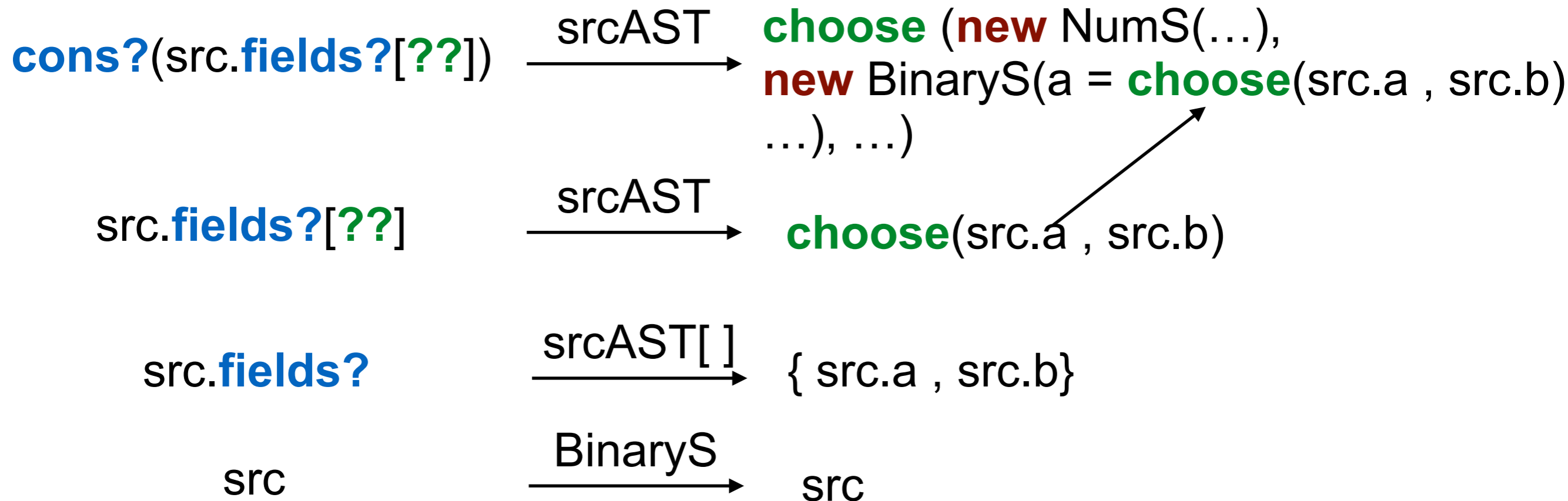
`src.fields?[??]` $\xrightarrow{\text{srcAST}}$ `choose(src.a , src.b)`

`src.fields?` $\xrightarrow{\text{srcAST}[]}$ `{ src.a , src.b }`

`src` $\xrightarrow{\text{BinaryS}}$ `src`

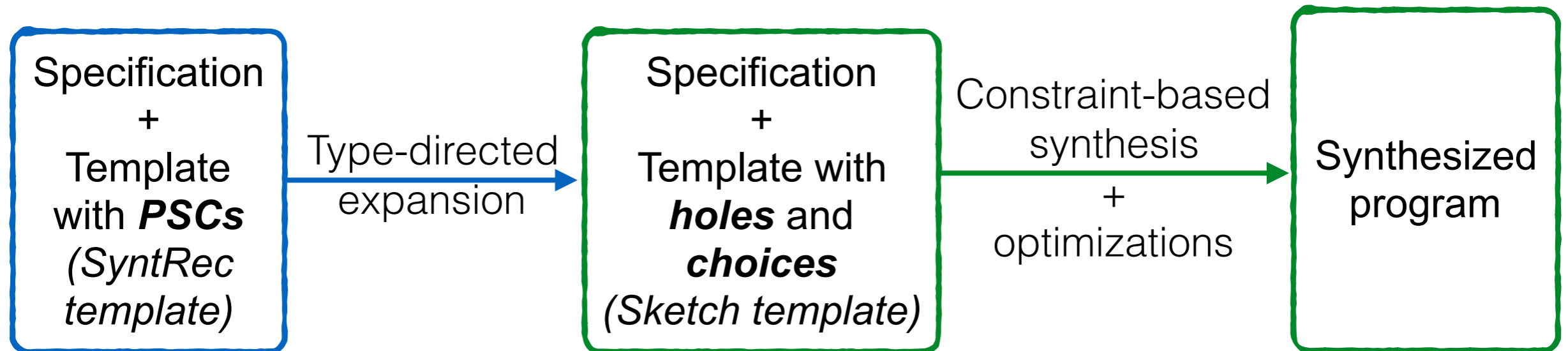
```
adt srcAST {  
  NumS { int v; }  
  TrueS { }  
  FalseS { }  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

Type-directed expansion



```
adt srcAST {  
  NumS { int v; }  
  TrueS { }  
  FalseS { }  
  BinaryS { opcode op; srcAST a; srcAST b; }  
  BetweenS { srcAST a; srcAST b; srcAST c; }  
}
```

Synthesis Approach

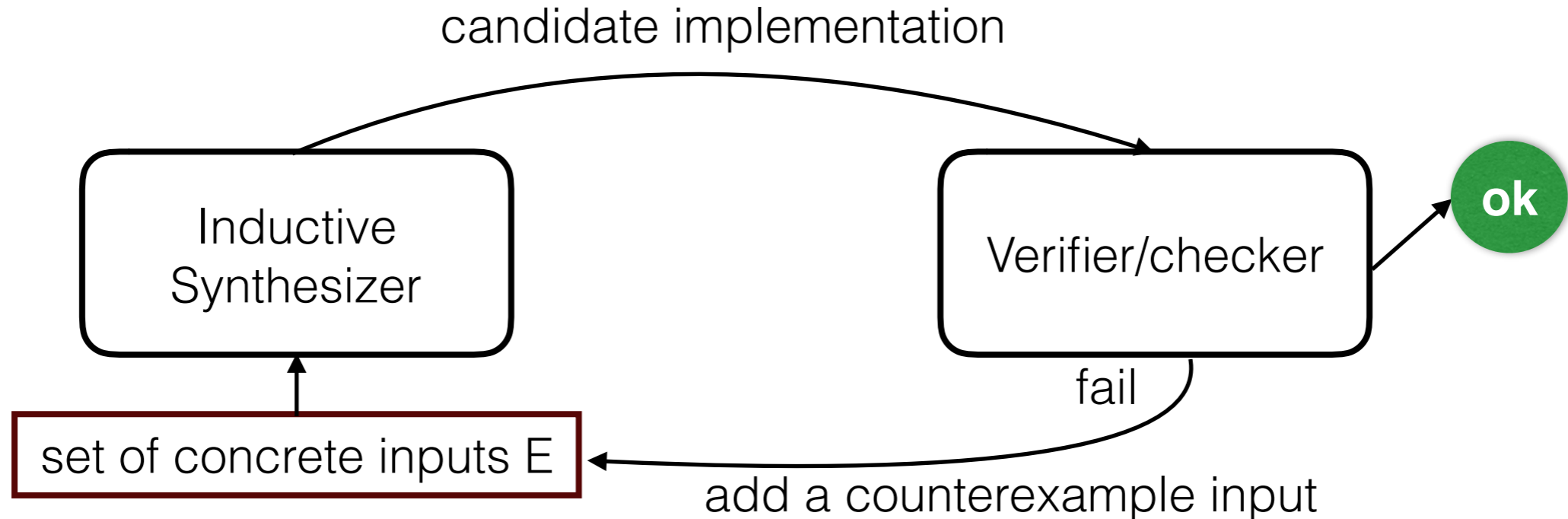


Constraint-based synthesis

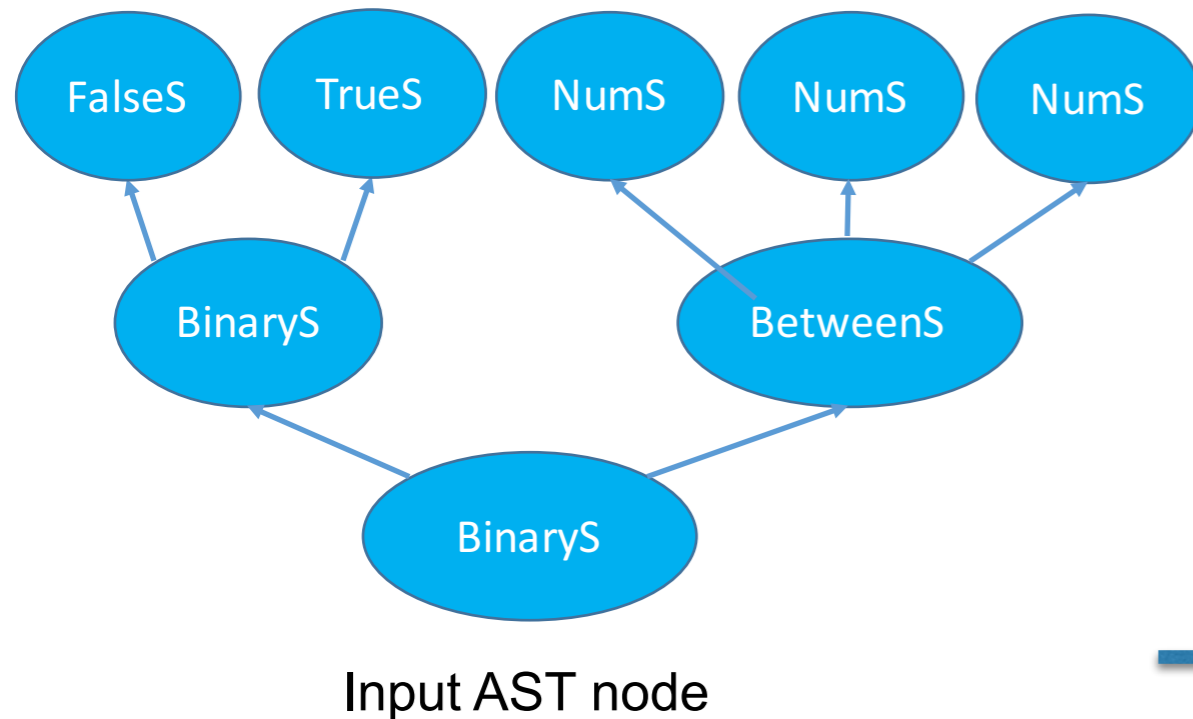
- Inlines function calls and unrolls loops

$$\exists c. \forall in. Q(in, c)$$

- Uses Counter Example Guided Inductive Synthesis (CEGIS)



Constraint-based synthesis



dstAST desugar (srcAST src)

switch (src)

case NumS:

return rcons(()→src .v)

case TrueS:

return rcons(()→ 0)

case FalseS:

return rcons(()→ 0)

case BinaryS:

dstAST a = desugar(src.a)

dstAST b = desugar(src.b)

return rcons(()→**choose**(a, b, src .op))

case BetweenS:

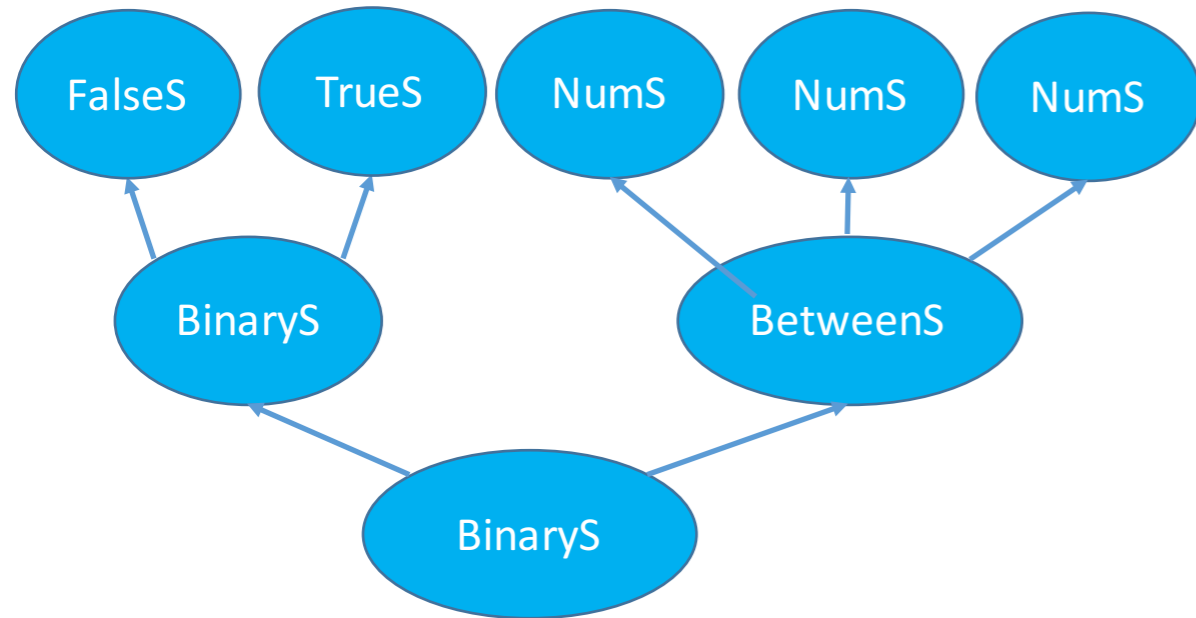
dstAST a = desugar(src.a)

dstAST b = desugar(src.b)

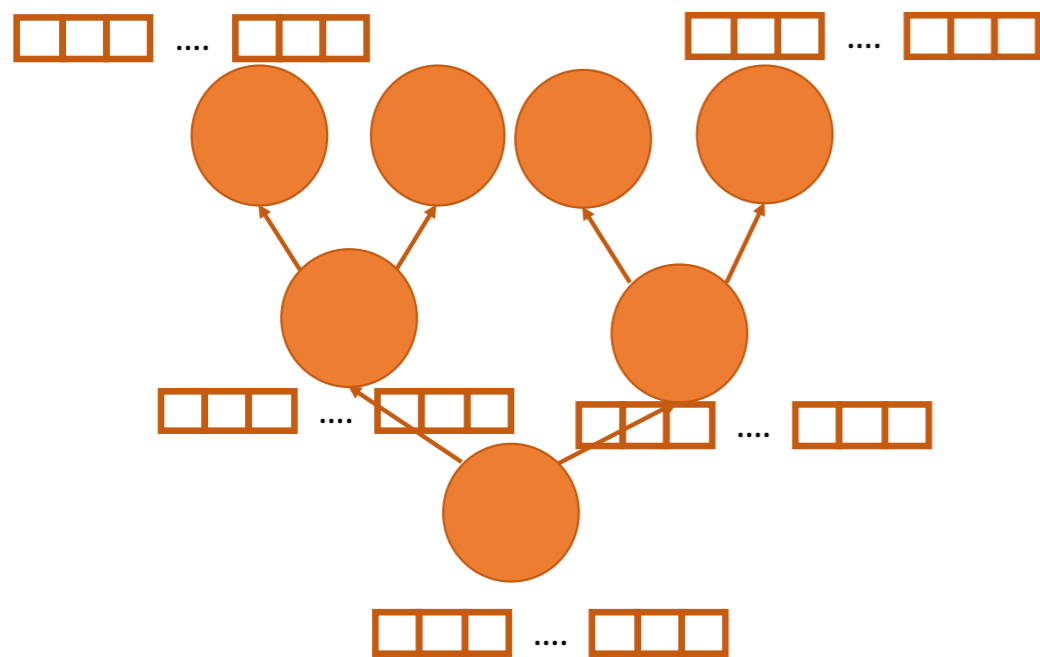
dstAST c = desugar(src.c)

return rcons(()→**choose**(a, b, c))

Constraint-based synthesis

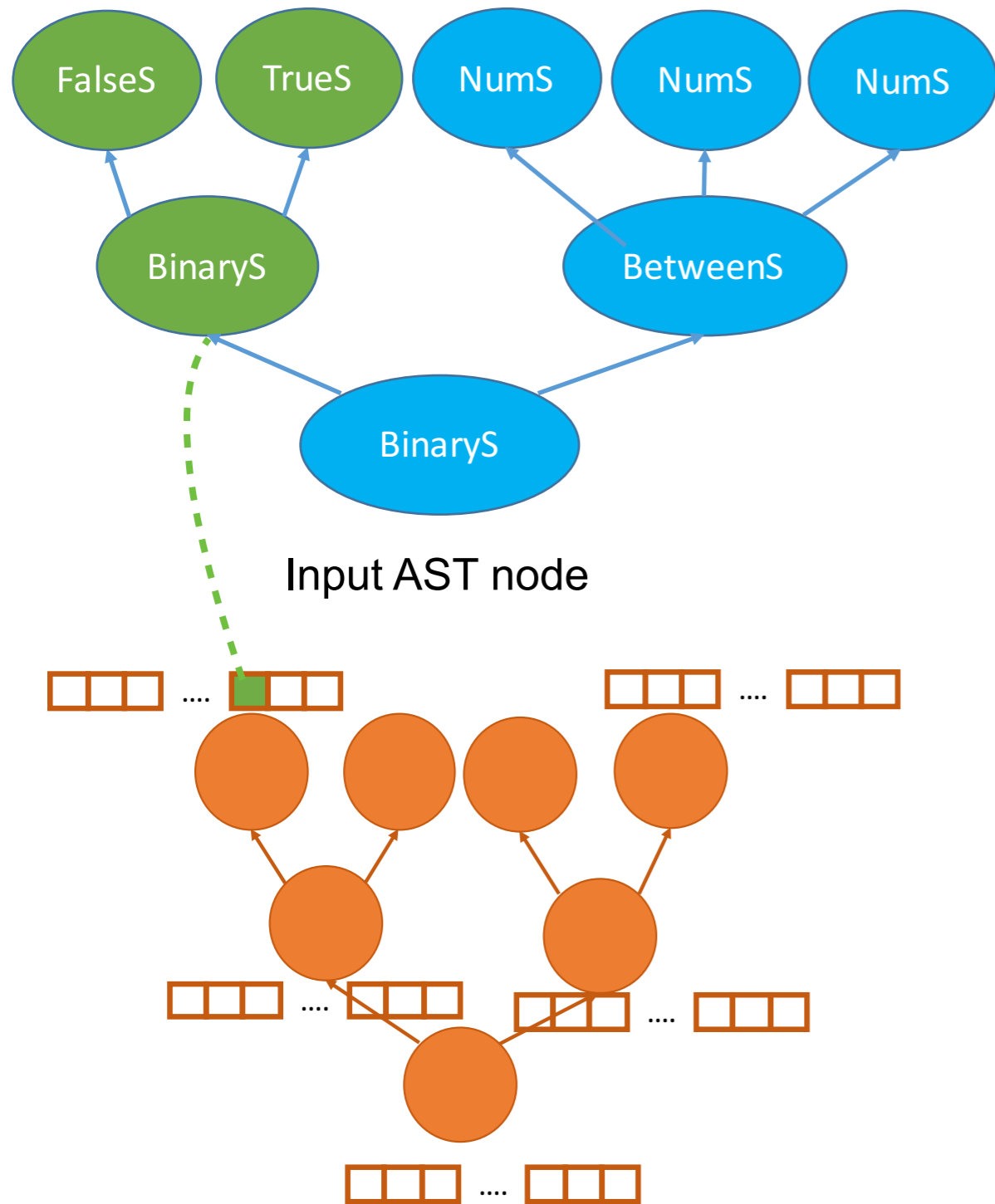


Input AST node



```
dstAST desugar (srcAST src)
switch (src)
  case NumS:
    return rcons(()→src .v )
  case TrueS:
    return rcons(()→ 0 )
  case FalseS:
    return rcons(()→ 0 )
  case BinaryS:
    dstAST a = desugar(src.a)
    dstAST b = desugar(src.b)
    return rcons(()→choose(a, b, src .op))
  case BetweenS:
    dstAST a = desugar(src.a)
    dstAST b = desugar(src.b)
    dstAST c = desugar(src.c)
    return rcons(()→choose(a, b, c ))
```

Constraint-based synthesis



```
dstAST desugar (srcAST src)
```

```
switch (src)
```

```
case NumS:
```

```
return rcons(()→src .v )
```

```
case TrueS:
```

```
return rcons(()→ 0 )
```

```
case FalseS:
```

```
return rcons(()→ 0 )
```

```
case BinaryS:
```

```
→ dstAST a = desugar(src.a)
```

```
dstAST b = desugar(src.b)
```

```
return rcons(()→choose(a, b, src .op))
```

```
case BetweenS:
```

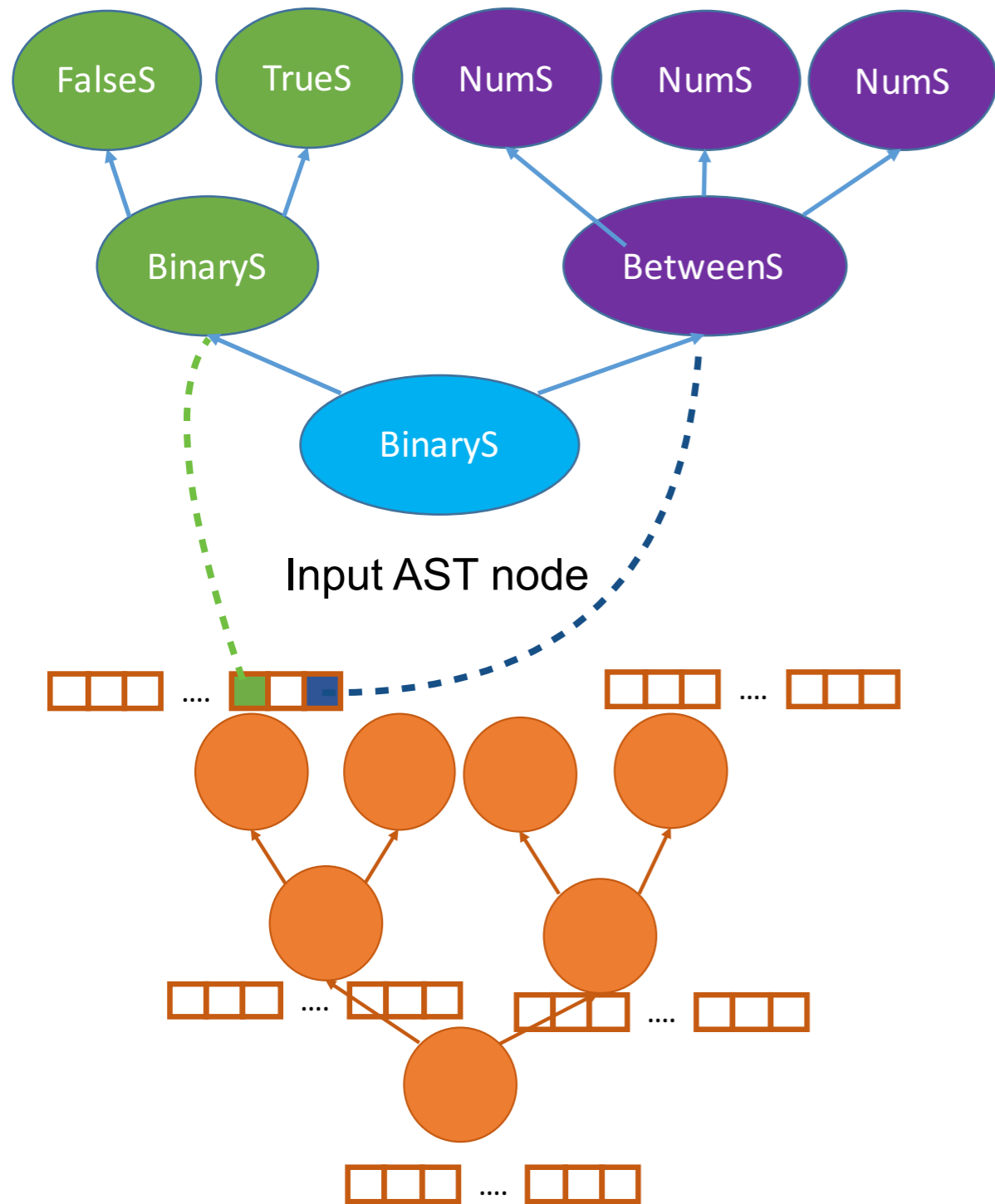
```
dstAST a = desugar(src.a)
```

```
dstAST b = desugar(src.b)
```

```
dstAST c = desugar(src.c)
```

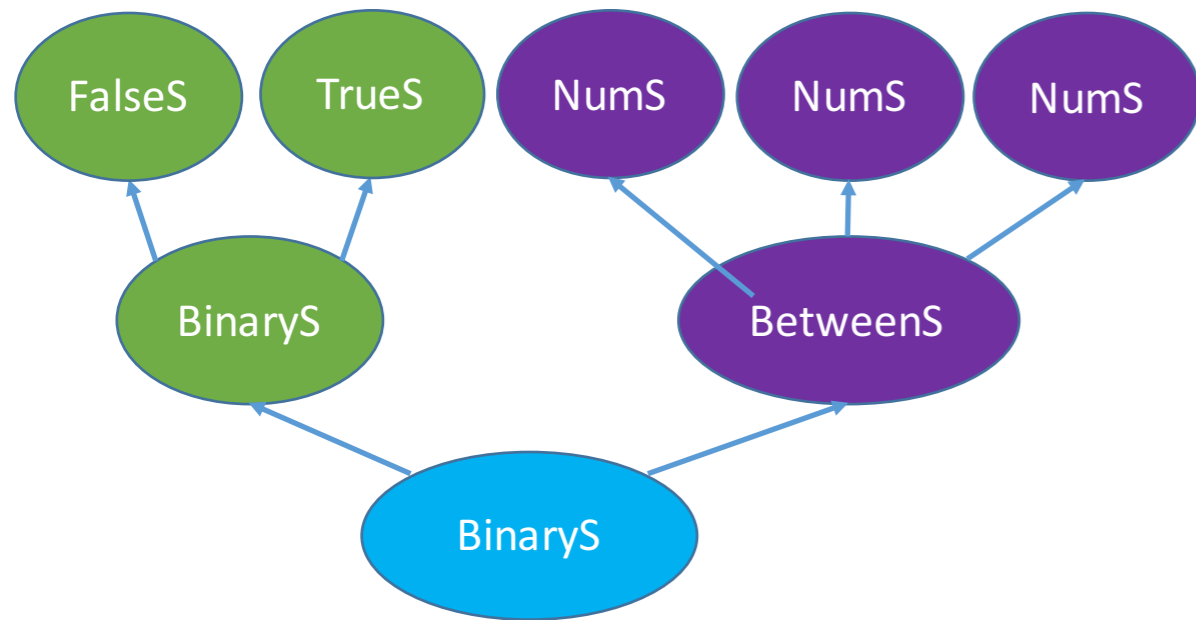
```
return rcons(()→choose(a, b, c ))
```


Constraint-based synthesis

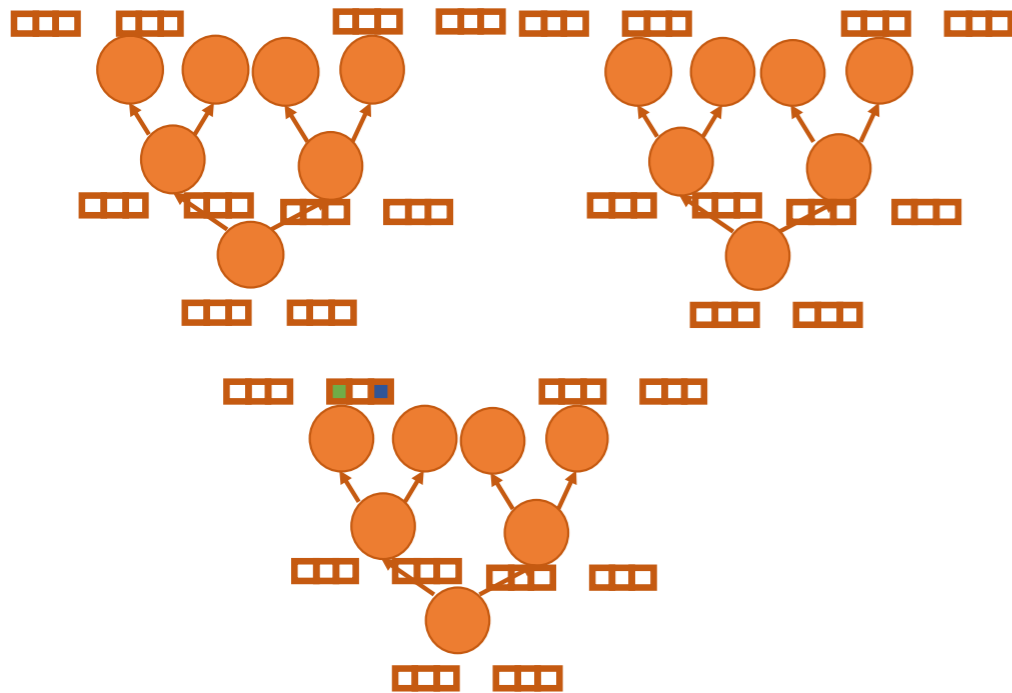


```
dstAST desugar (srcAST src)
  switch (src)
  case NumS:
    return rcons(()→src .v )
  case TrueS:
    return rcons(()→ 0 )
  case FalseS:
    return rcons(()→ 0 )
  case BinaryS:
    dstAST a = desugar(src.a)
    dstAST b = desugar(src.b)
    return rcons(()→choose(a, b, src .op))
  case BetweenS:
    dstAST a = desugar(src.a)
    dstAST b = desugar(src.b)
    dstAST c = desugar(src.c)
    return rcons(()→choose(a, b, c ))
```

Constraint-based synthesis



Input AST node



```
dstAST desugar (srcAST src)
```

```
switch (src)
```

```
case NumS:
```

```
return rcons(()→src .v )
```

```
case TrueS:
```

```
return rcons(()→ 0 )
```

```
case FalseS:
```

```
return rcons(()→ 0 )
```

```
case BinaryS:
```

```
dstAST a = desugar(src.a)
```

```
dstAST b = desugar(src.b)
```

```
return rcons(()→choose(a, b, src .op))
```

```
case BetweenS:
```

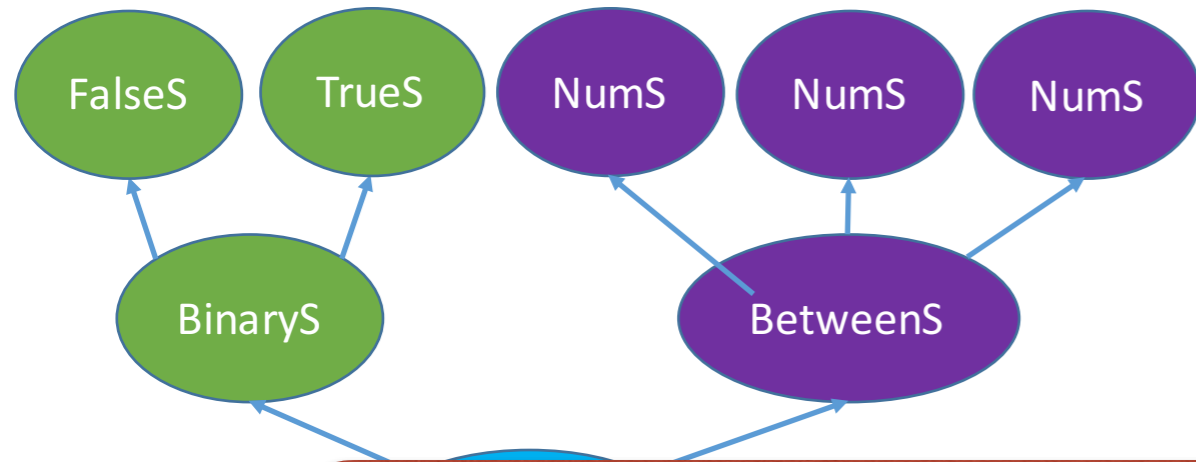
```
dstAST a = desugar(src.a)
```

```
dstAST b = desugar(src.b)
```

```
dstAST c = desugar(src.c)
```

```
return rcons(()→choose(a, b, c ))
```

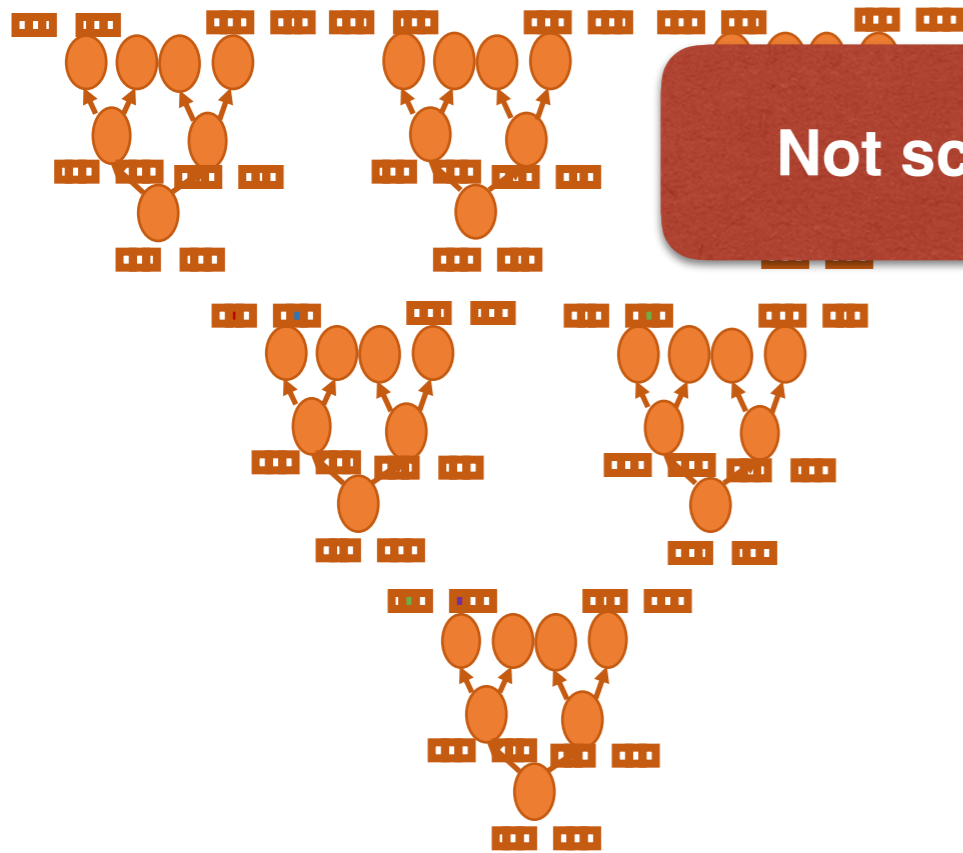
Constraint-based synthesis



```
dstAST desugar (srcAST src)  
switch (src)  
  case NumS:  
    return rcons(()→src .v )  
  case TrueS:  
    return rcons(()→ 0 )
```

Synthesizer needs to reason about all variants together

Input AST node



```
dstAST a = desugar(src.a)  
dstAST b = desugar(src.b)  
return rcons(()→choose(a, b, src .op))
```

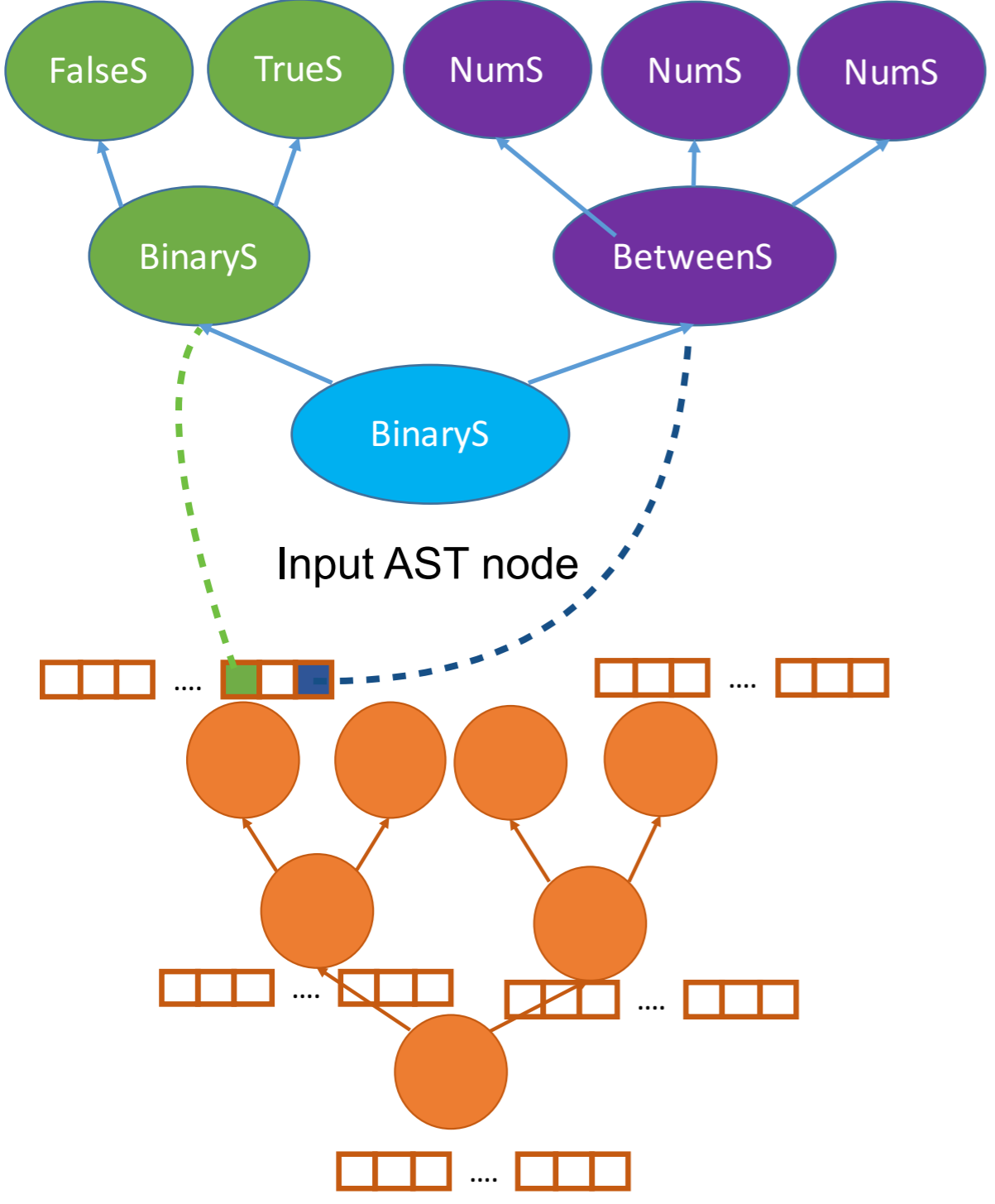
Not scalable for ADTs with many cases

```
dstAST a = desugar(src.a)  
dstAST b = desugar(src.b)  
dstAST c = desugar(src.c)  
return rcons(()→choose(a, b, c ))
```

Inductive Decomposition

- Use specification as an invariant to abstract recursive calls

Inductive Decomposition

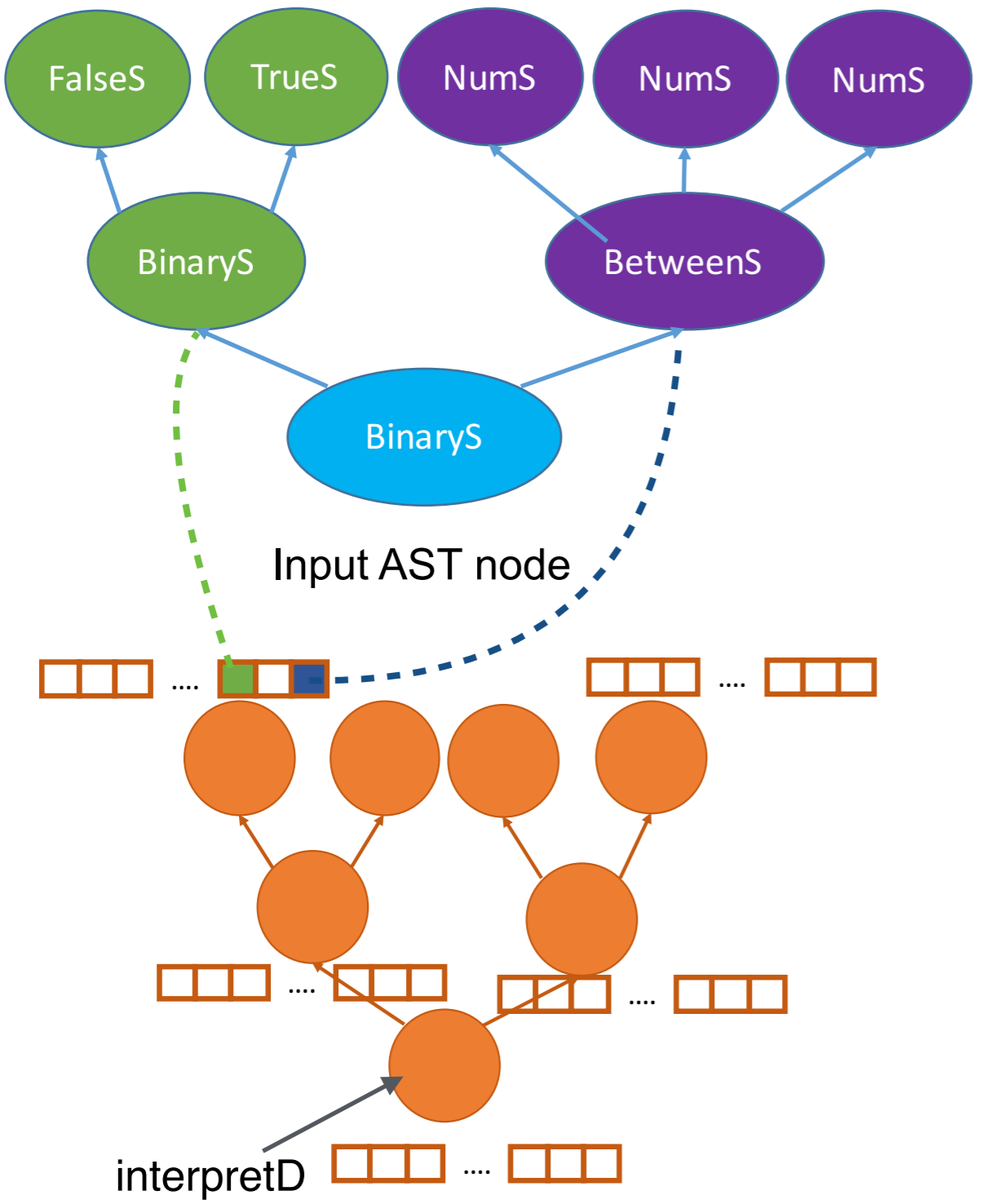


```

int interpretD (dstAST dst)
  switch (dst)
  case NumD:
    return dst.v
  case BoolD:
    return dst.v
  case Binary:
    base a = interpretD(dst.a)
    base b = interpretD(dst.b)
    return compute(dst.op, a, b)
  
```

$\text{interpretS}(s) == \text{interpretD}(\text{desugar}(s))$

Inductive Decomposition

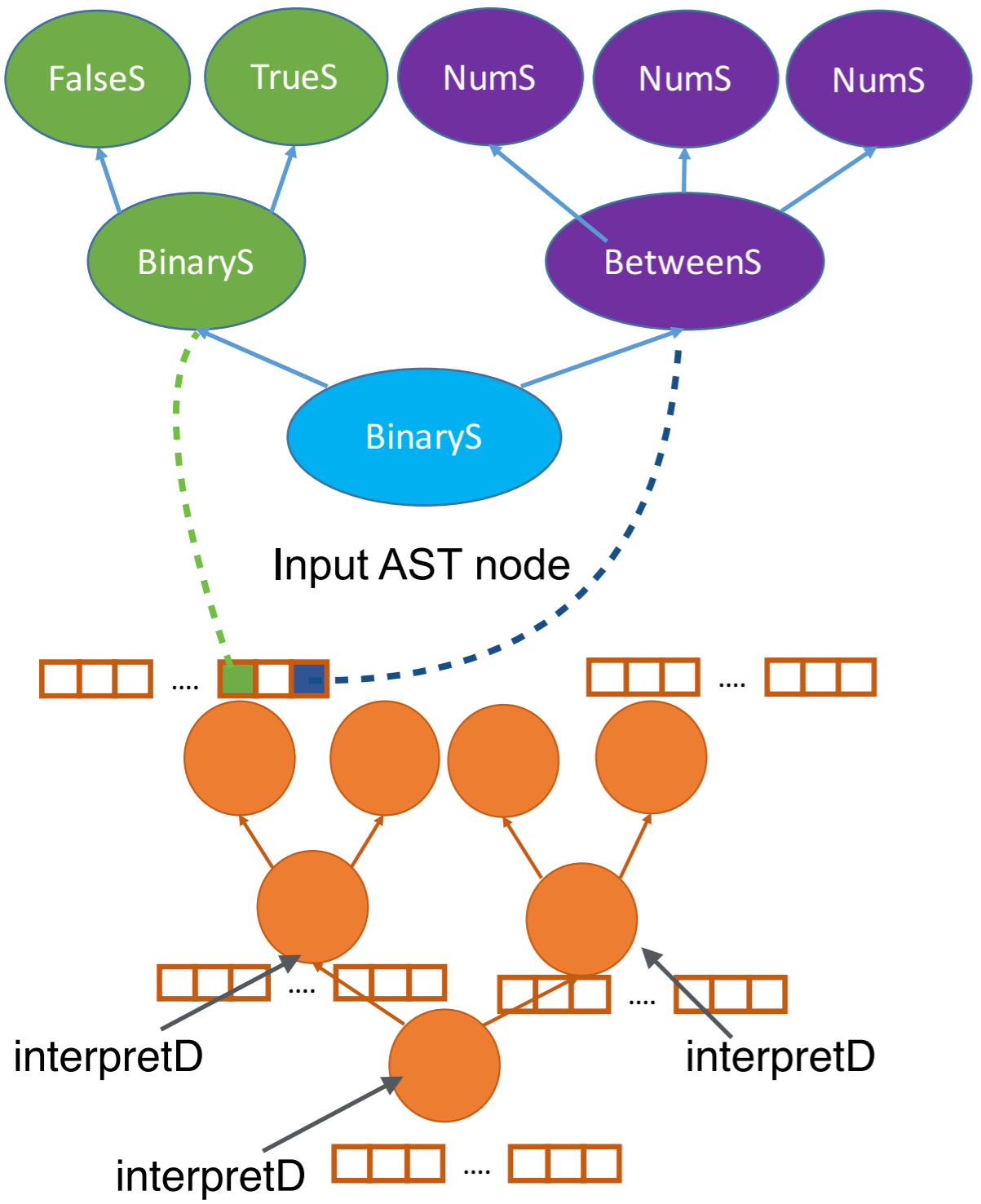


```

int interpretD (dstAST dst)
  switch (dst)
  case NumD:
    return dst.v
  case BoolD:
    return dst.v
  case Binary:
    base a = interpretD(dst.a)
    base b = interpretD(dst.b)
    return compute(dst.op, a, b)
  
```

$interpretS(s) == interpretD(desugar(s))$

Inductive Decomposition

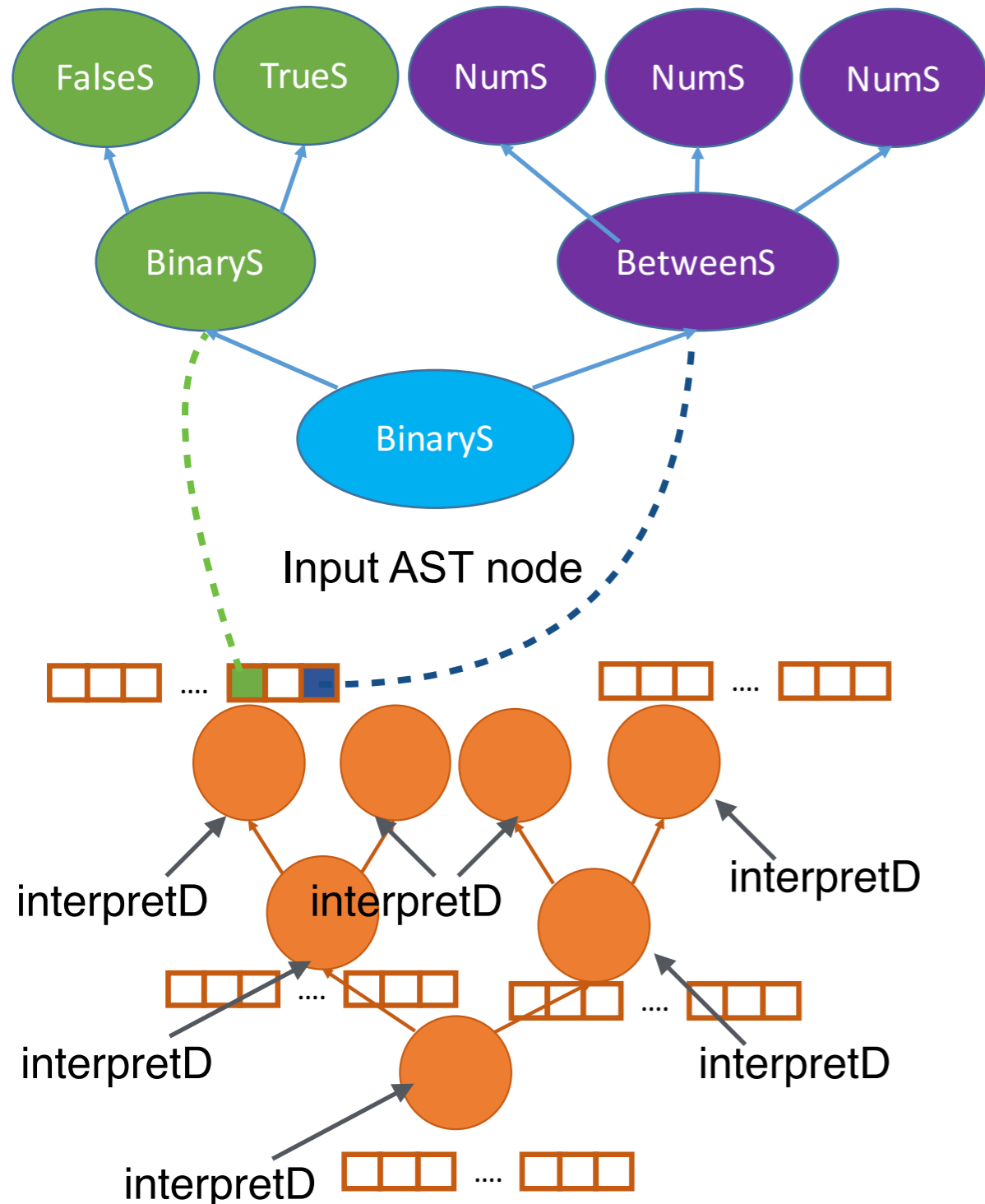


```

int interpretD (dstAST dst)
  switch (dst)
  case NumD:
    return dst.v
  case BoolD:
    return dst.v
  case Binary:
    base a = interpretD(dst.a)
    base b = interpretD(dst.b)
    return compute(dst.op, a, b)
  
```

$interpretS(s) == interpretD(desugar(s))$

Inductive Decomposition



```

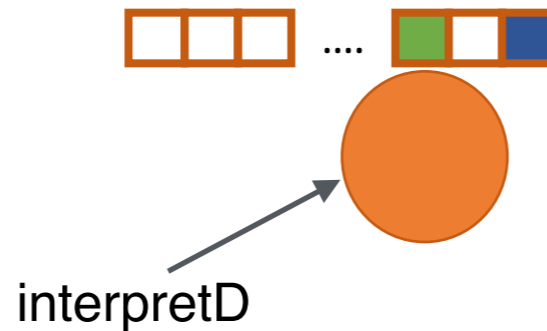
int interpretD (dstAST dst)
  switch (dst)
  case NumD:
    return dst.v
  case BoolD:
    return dst.v
  case Binary:
    base a = interpretD(dst.a)
    base b = interpretD(dst.b)
    return compute(dst.op, a, b)
  
```

$\text{interpretS}(s) == \text{interpretD}(\text{desugar}(s))$

Inductive Decomposition

$$\text{interpretS}(s) == \text{interpretD}(\text{desugar}(s))$$

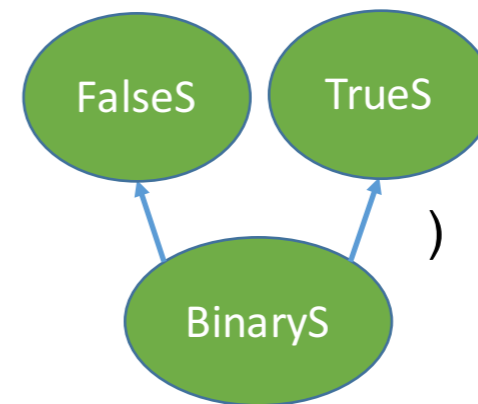
Case 1: Node flows directly into interpretD



`interpretD ()`

`==`

`interpretS (`

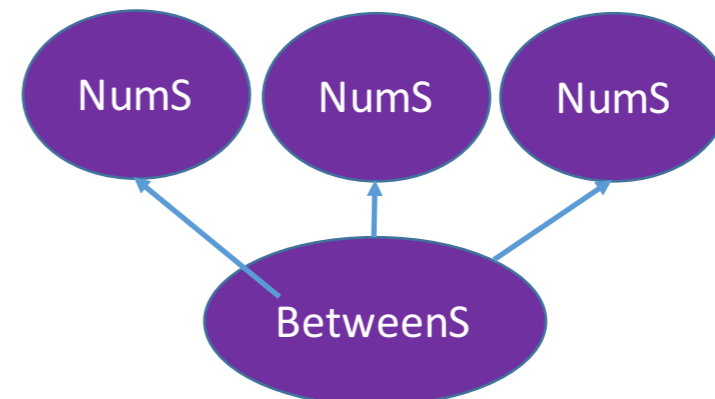


)

`interpretD ()`

`==`

`interpretS (`

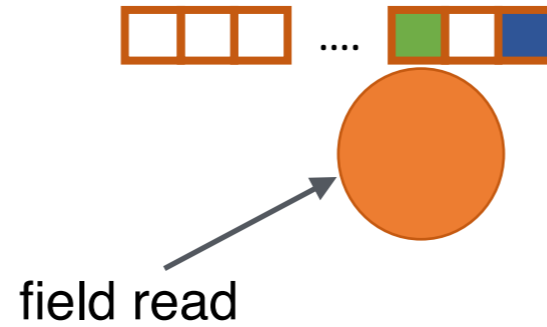


)

Inductive Decomposition

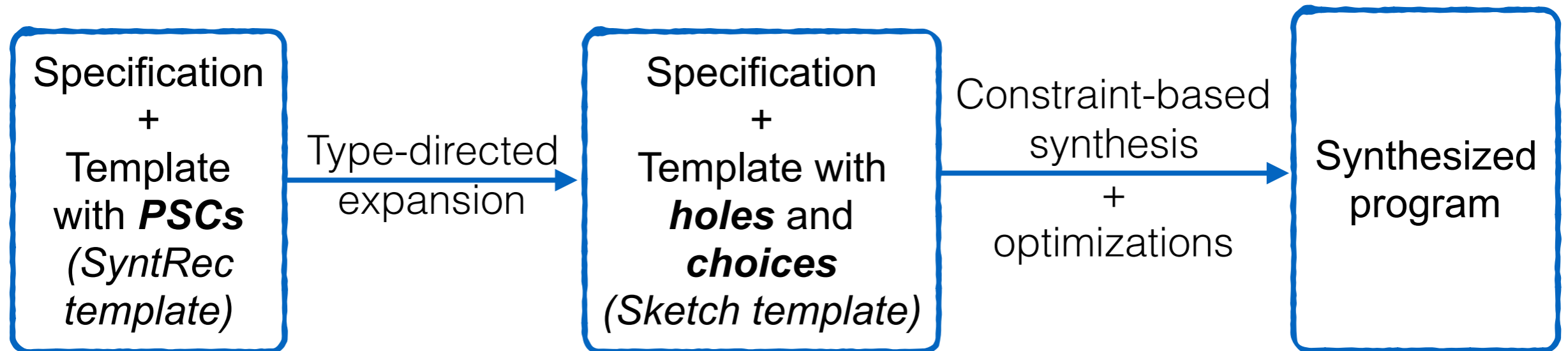
$\text{interpretS}(s) == \text{interpretD}(\text{desugar}(s))$

Case 2: Node flows into other nodes



Revert back to inlining the desugar calls

Synthesis Approach



Evaluation

- 23 benchmarks across various domains

Desugaring

List

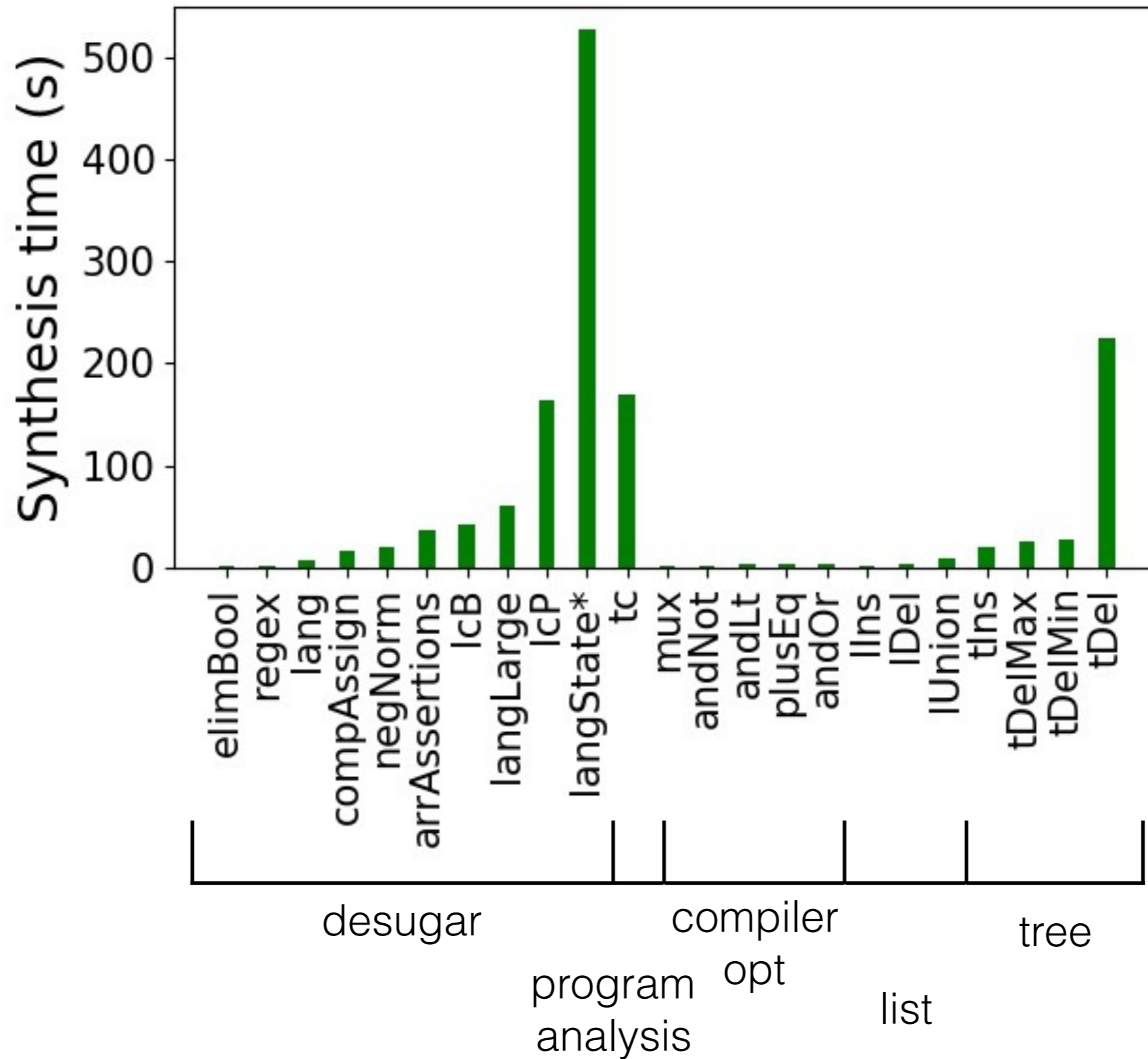
Tree

Program
Analysis

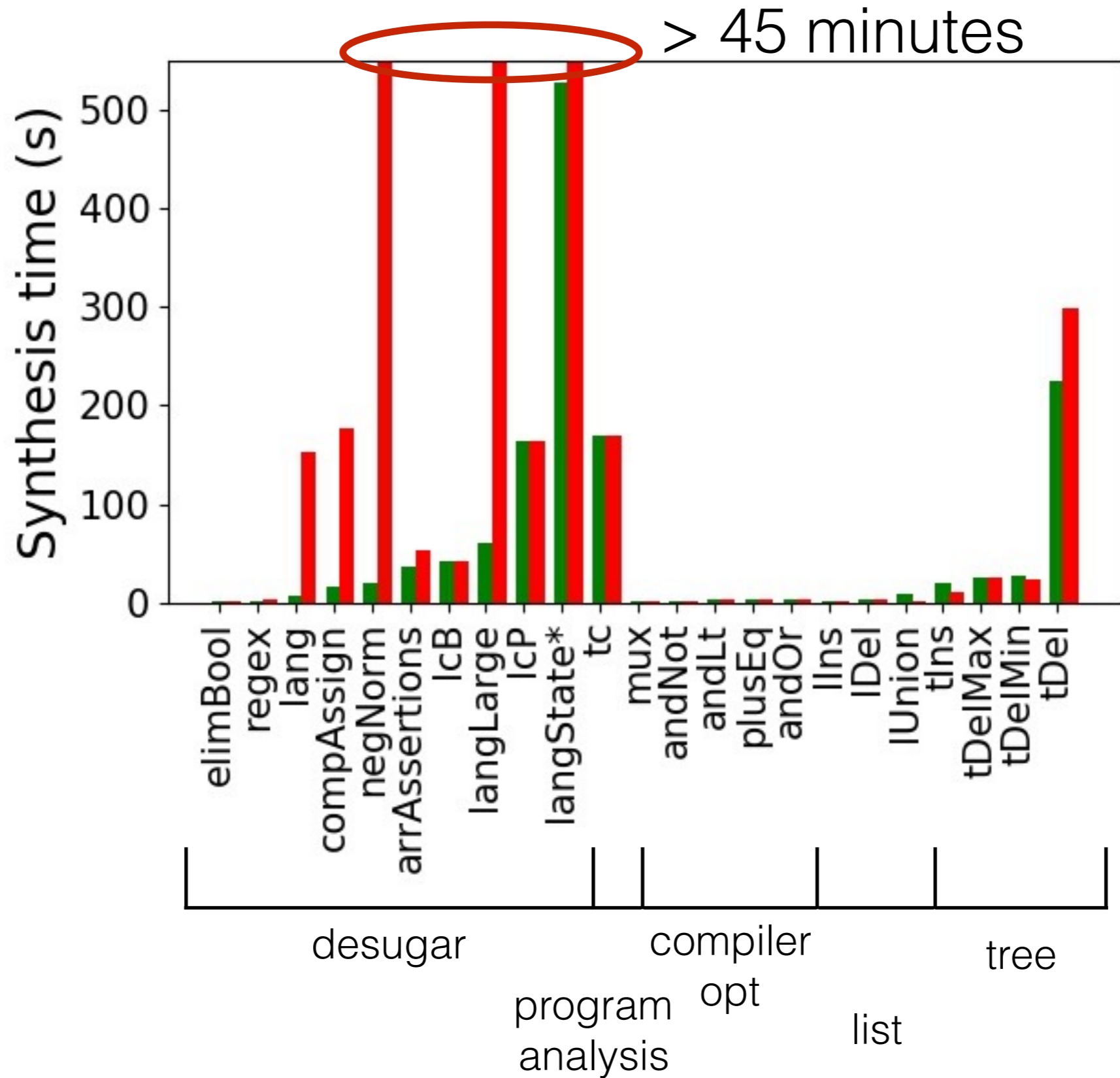
Compiler
optimizations

From only 4 generic library templates

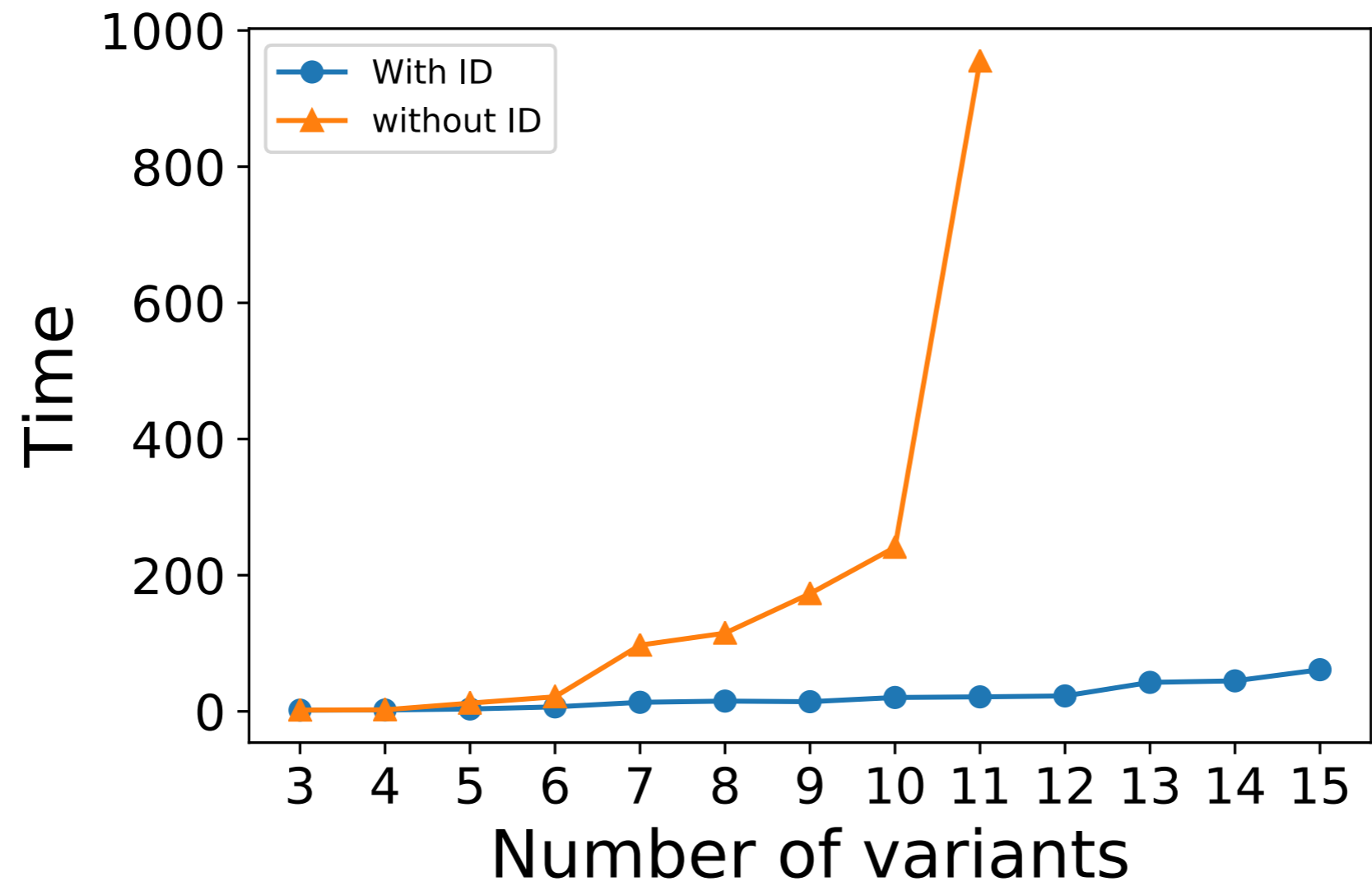
Evaluation



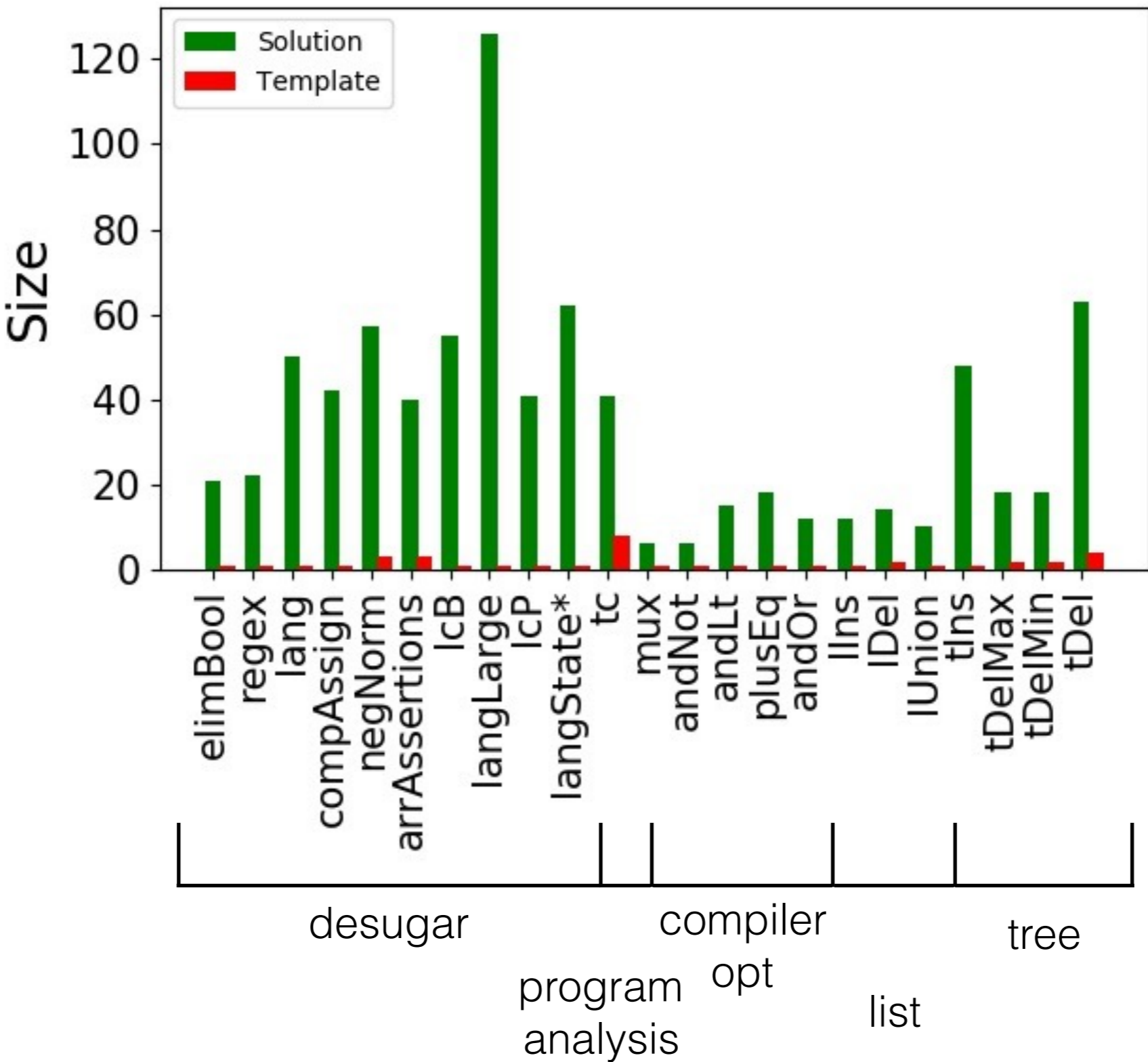
Evaluation



Evaluation



Evaluation



Summary

- A system to synthesize transformations on Algebraic Data Types from high level ***reusable templates***
- Uses a combination of type inference and constraint solving
- ***Inductive decomposition*** optimization to improve the scalability of synthesis of recursive functions
- Can synthesize complex functions like desugaring

